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MEMORANDUM REPORT BRL-MR-3428

DETERMINATION OF HEAT TRANSFER
COEFFICIENT IN A GUN BARREL
FROM EXPERIMENTAL DATA

William F. Donovan

January 1985

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TABLE OF CONTENTS

	Page
LIST OF ILLUSTRATIONS.....	5
LIST OF TABLES.....	7
I. INTRODUCTION.....	9
II. PROCEDURE.....	10
A. General Statement.....	10
B. Application to a Gun Barrel.....	11
C. Wall Surface Temperature.....	13
III. RESULTS.....	30
IV. CONCLUSIONS.....	30
REFERENCES.....	35
APPENDIX A	37
APPENDIX B	51
APPENDIX C.....	63
APPENDIX D.....	69
APPENDIX E.....	79
APPENDIX F.....	87
LIST OF SYMBOLS.....	91
DISTRIBUTION LIST.....	93

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LIST OF ILLUSTRATIONS

Figure		Page
1	Schematic of Infinitely Long Cylinder.....	12
2	Wall Surface Temperature Gradient.....	14
3	Graphical Determination of T_1^1	15
4	Graphical Determination of T_1^3	16
5	Graphical Determination of T_1^5	17
6	Graphical Determination of T_1^7	18
7	Graphical Determination of T_1^9	19
8	Schmidt Plot for Initial Subinterval from 0 to 1.....	23
9	Schmidt Plot for Time Interval from 1 to 3.....	24
10	Schmidt Plot for Time Interval from 3 to 5.....	25
11	Schmidt Plot for Time Interval from 5 to 7.....	26
12	Schmidt Plot for Time Interval from 7 to 9.....	27
13	Experimental Wall Temperature History for Special Propellant Round.....	31
14	Driving Gas Temperature Profiles.....	32
15	Heat Transfer Coefficient Profiles.....	33
A-1	Schmidt Plot for Schematic Slab Temperature Profile.....	39
A-2	Schmidt Plot for Sample Slab Problem.....	48
B-1	Schmidt Plot Schematic for Cylindrical Wall Temperature Profile.....	53

LIST OF TABLES

Table		Page
1	ALGEBRAIC SPECIFICATION OF T_{1n}	20
2	ALGEBRAIC SPECIFICATION OF T_{2n}	20
3	ALGEBRAIC SPECIFICATION OF T_{0n} FOR $m = \text{CONSTANT}$	28
4	ALGEBRAIC SPECIFICATION OF T_{0n} FOR $m \neq \text{CONSTANT}$	29
A-1	STEPPING PROGRESSION IN TEMPERATURE TIME PARAMETERS FOR SLAB.....	40
A-2	DEFINITION OF BOUNDARY CONDITIONS FOR SAMPLE SLAB PROBLEM...	44
B-1	STEPPING PROGRESSION IN TEMPERATURE TIME PARAMETERS FOR CYLINDER.....	54
B-2	DEFINITION OF BOUNDARY CONDITIONS FOR SAMPLE CYLINDER PROBLEM.....	58
C-1	DEFINITION OF BOUNDARY CONDITIONS FOR SAMPLE PLANE WALL PROBLEM.....	66
D-1	DEFINITION OF BOUNDARY CONDITIONS FOR EXPERIMENTAL PROPELLANT ROUND.....	72

I. INTRODUCTION

The particular problem of estimating gun barrel temperature profiles in the vicinity of high energy gas flow has been examined experimentally by local investigators, and the general problem of mathematically constrained, ^{2,3,4} unsteady, high temperature heat flux is treated in the open literature. Historically, the preliminary layout of liquid propellant rocket combustion chambers has often employed the Schmidt diagram^{5,6} to estimate the critical metal temperatures in the structure. This is developed as a finite difference approximation of the second order, first degree partial differential equation of physics in heat flow context and is usually presented graphically. The graphical analysis is an alternative to the LaPlace Transform treatment which is unwieldy in execution. It also competes with the differential analyzer technique. Rigorous solutions to the second order axisymmetric problem in the form of mapped finite element presentations of the detailed transient flow phenomena are promised for the proximate future.

A specific and comprehensive solution to the barrel problem has recently been delivered in the form of mathematical presentation by Polk,⁹ and this in the explicitly usable form of a moderate level computer program (Hewlett-Packard 9845) for direct application. The Polk treatise is not currently in BRL report format, however, and the program is still being refined. A

- ¹ T. L. Brosseau, "An Experimental Method for Accurately Determining Temperature Distribution and the Heat Transferred in Gun Barrels," BRL-R-1740, September 1974. AD #B000171L.
- ² Mark W. Zemansky, Heat and Thermodynamics, McGraw-Hill Book Company Inc., New York, 1957.
- ³ Max Jacob, Heat Transfer, Vol. 1, John Wiley and Sons, New York, 1949.
- ⁴ E. F. Quigley, "One Dimensional Transient Temperature and Stress Distribution Produced in 0.375- and 0.500- inch Thick 7075A1-T6 Flat Plates by Fourteen Nuclear Thermal Environment," BRL-MR-2173, April 1972. AD #901995.
- ⁵ Frank Kreith, Principles of Heat Transfer, International Text Book Company, Scranton, PA., 1963.
- ⁶ George P. Sutton, Rocket Propulsion Elements, John Wiley and Sons, New York, 1956.
- ⁷ Theodore V. Karman and Maurice A. Biot, Mathematical Methods in Engineering, McGraw-Hill Book Company Inc., New York 1940.
- ⁸ P. L. Versteegen and F. D. Varcolik, "Heat Transfer Studies in Gun Tubes," ARBRL-CR-00393 (Science Applications Inc., McLean, VA.) March 1979. AD #A069649
- ⁹ J. F. Polk, "An Algorithm for Heat Transfer in Gun Barrels," Transactions of the Twenty-Fifth Conference of Army Mathematicians, ARO Report 80-1, 1980.

complete FORTRAN program, based on a Calspan reference,¹⁰ is also available but has yet to be introduced into the local Control Data Corporation facility.

In direct graphical exposition, the Schmidt plot consists of a large scale drafting wherein the results are recovered as measured values rather than discrete numbers. This report offers the details of a desk top calculator (Hewlett-Packard 97) procedure algebraically transposed from the finite difference scheme to calculate heat transfer coefficients in a ballistics environment from an overdetermined set of equations. The data is from experiment, and an implicit assumption is that the driving gas temperature is constant over the selected time interval of the calculation. The appropriate driving gas temperature can then be determined by regressive substitution.

Thermodynamic units always deserve a special note. The examples are presented in the International System of Units, the British, and in normalized parameters. The British units are employed simply because the materials properties values are most widely available in this system, and it therefore offers direct and convenient application. The SI is proposed as a standard, and the normalized borrows from the Jacob-Hawkins³ practice with an additional modification to eliminate geometric scale factors.

II. PROCEDURE

A. General Statement

The differential equation describing one dimensional, unsteady, conductive heat flow through a solid is

$$\frac{1}{a} \frac{\partial T}{\partial t} = \frac{\partial^2 T}{\partial x^2} \quad (\text{rectangular slab}). \quad (1)$$

where a is thermal diffusivity,
 T is temperature,
 t is time,
 x is distance.

Approximate solutions to the differential equations can be obtained by solving the finite difference analogue.

$$\frac{1}{a} \frac{\Delta T}{\Delta t} = \frac{\Delta^2 T}{\Delta x^2} \quad (2)$$

¹⁰ "CYCOND" Program, and "HTC" Program, communication via Mr. Kovacs, DRDAR-SE, Picatinny Arsenal.

with Δt equal to the finite difference in time,
 Δx^2 equal to the finite difference in distance,
 $\Delta_t T$ equal to the time variable effecting a change in T , and
 $\Delta_x T$ equal to the distance variable effecting a change in T .

By then defining "t" as the number of time increments (Δt), and "n" as the distance increment, the direct application form of the equation becomes

$$\frac{1}{a} \frac{T_n(t+1) - T_n(t)}{\Delta t} = \frac{T_{(n+1)}(t) - 2 T_n(t) + T_{(n-1)}(t)}{\Delta x^2} \quad (3)$$

Note: Throughout this report, the notation $T_n t$ and $T_n(t)$ will be used interchangeably. Parenthesis will be used only when added clarity is necessary.

Appendix A transcribes the finite differences to algebraic formulation and illustrates the Schmidt plot by numerical example.

In cylindrical coordinates the finite difference equation becomes

$$\frac{1}{a} \frac{T_n(t+1) - T_n(t)}{\Delta t} = \frac{1}{r^2} \left(\frac{T_{(n+1)}(t) + T_{(n-1)}(t) - 2 T_n(t)}{\Delta j^2} \right) \quad (4)$$

where $r = e^j$,

and $\Delta j = \frac{\Delta r}{r}$,

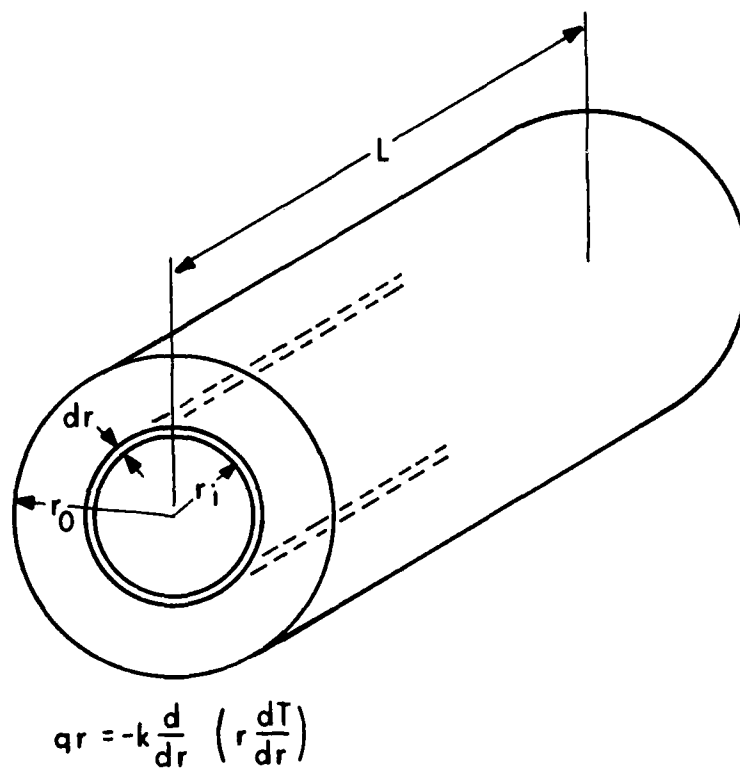
for any radius "r" with "j" defined in terms of "r".

Appendix B presents the cylindrical transcription and a numerical example for illustration.

B. Application to a Gun Barrel

The gun barrel is represented as a long thick-walled annular cylinder, Figure 1, with a suddenly imposed high temperature gas flowing through the bore. To estimate the wall temperature gradient, three assumptions are required:

1. A gas temperature history.
2. Unvalued properties of the medium.
3. Radiation and convection accountable by the modification of the value for unit surface conductance.



where

r_i is the inner cylinder radius

r_o is the outer cylinder radius

Figure 1. Schematic of Infinitely Long Cylinder

C. Wall Surface Temperature

The procedure used to develop the equations which specify the temperature of the face of a slab after exposure to a high temperature gas consists of:

1. Construction of the Schmidt plot, which is geometrically defined in terms of selected gas and metal properties; i.e., the heat transfer coefficient (\bar{h}), the reference temperature (T_o), the conductivities of the gas and the metal (k), and the diffusivity of the metal (a).
2. Transformation from the geometric to the equivalent algebraic expression.

In this context, as shown in Figure 2.

$$\Delta T_o = T_o - T_n.$$

$$m = \frac{\Delta x}{\Delta x + \Delta x_o}, \quad \text{or} \tag{5}$$

$$= \frac{1}{1 + (\Delta x_o / \Delta x)}; \tag{6}$$

where $\Delta x_o = \frac{k}{h}$ by construction of the Schmidt plot and

$$\Delta x = (2a\Delta t)^{1/2}, \tag{7}$$

where $\Delta t = \frac{\text{duration of heat exposure}}{\text{number of time intervals}}.$

For the gun problem, the duration of the heat exposure may be determined from the in-bore projectile trajectory history and an adiabatic flame temperature established from a definition of the propellant composition. These are tenuous criteria, of course, but are within the existing "state of the art." From Figure 2 and Table 1, the temperatures at the wall (Plane 1) are algebraically fixed for the first ten time intervals in terms of equivalent Schmidt plot distances corresponding to the specific thermal resistances on each side of the wall plane. Table 1, obtained from Figures 3 through 7, presents the algebraic resolution of the temperature profile for the interstitial planes. Table 2 gives the corresponding temperatures for the second plane - based on the same reasoning. These particular formulae neglect the influence of curvature since the wall penetration (Δx) approaches zero.

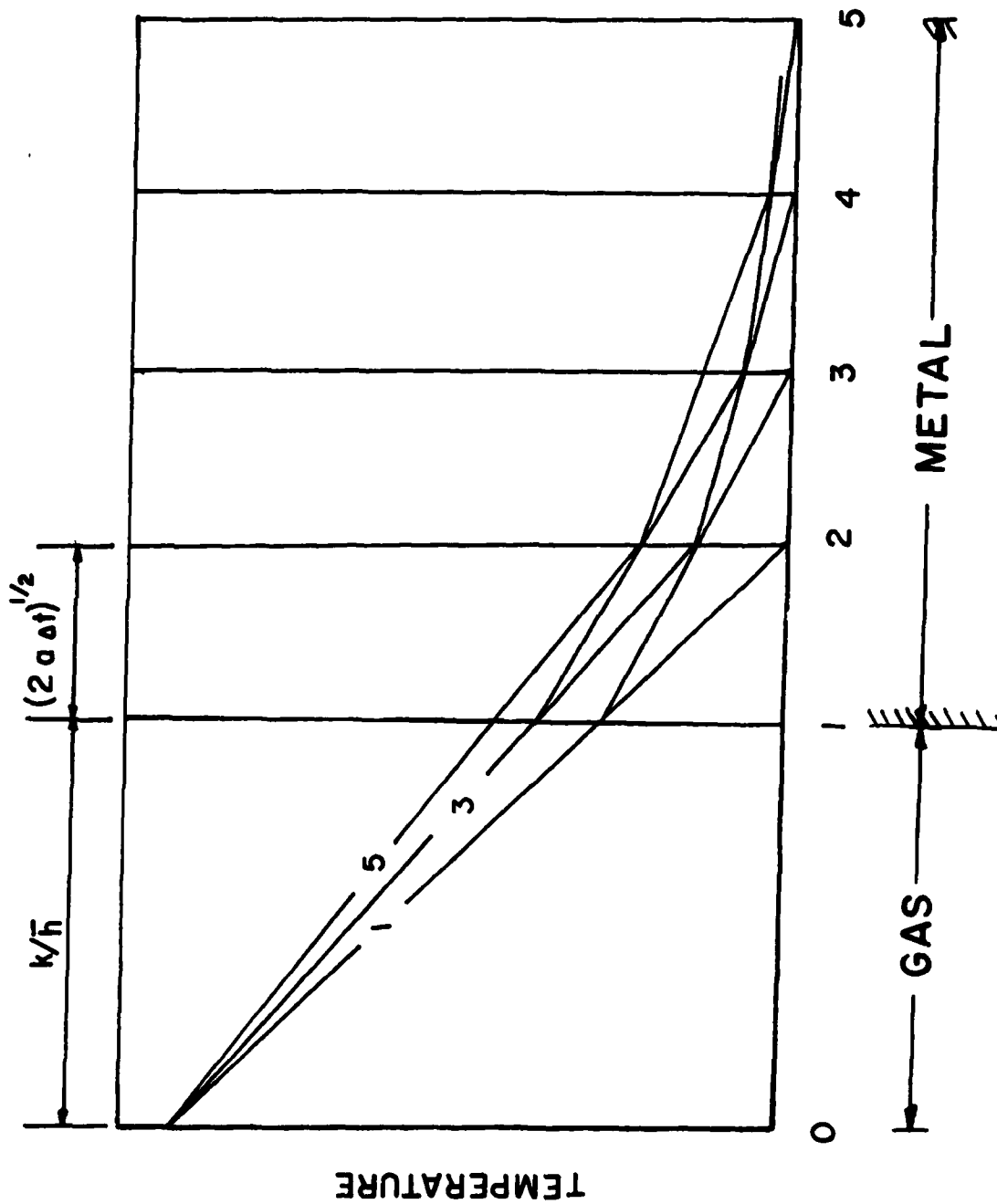


Figure 2. Wall Surface Temperature Gradient

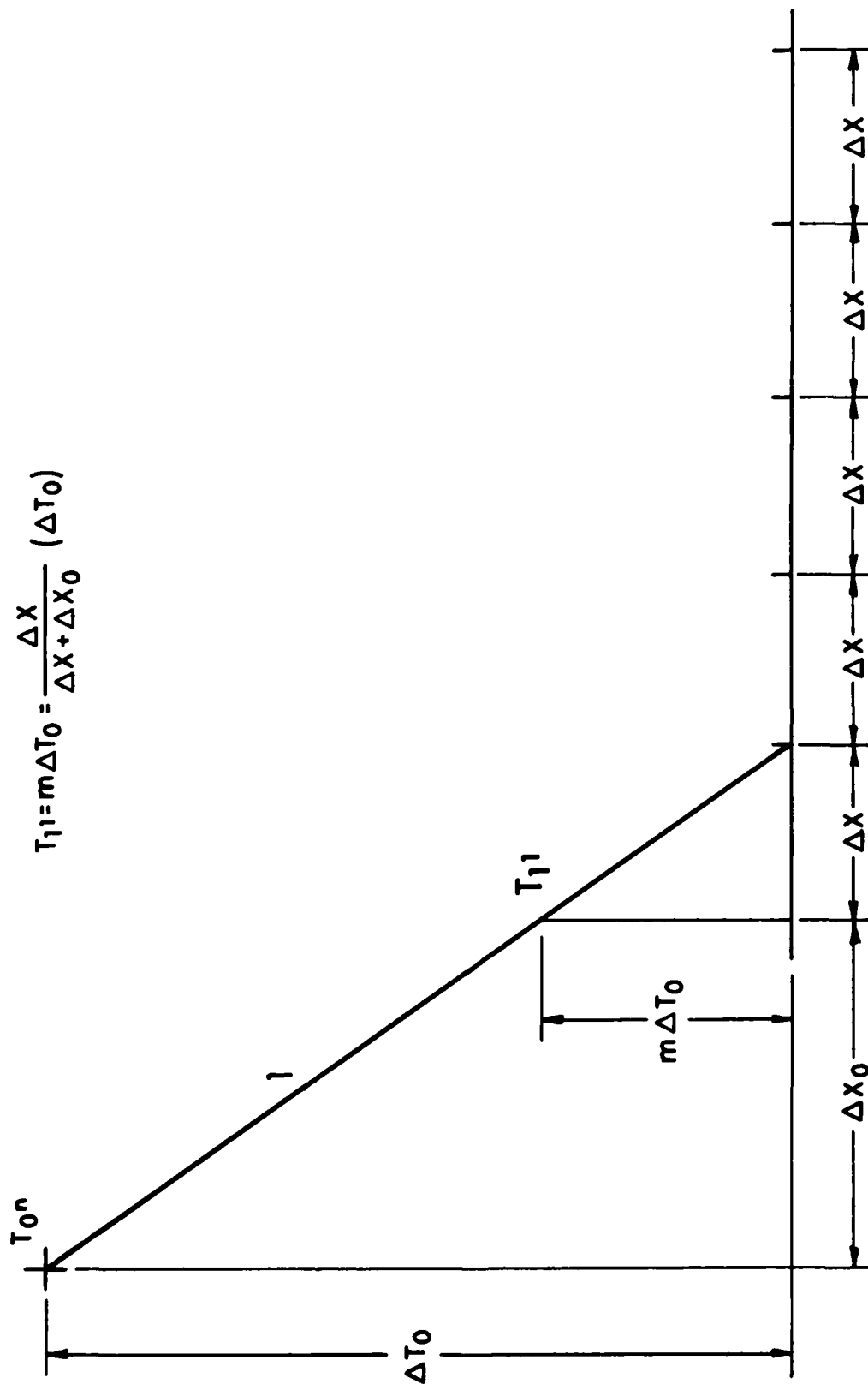


Figure 3. Graphical Determination of T_1^l

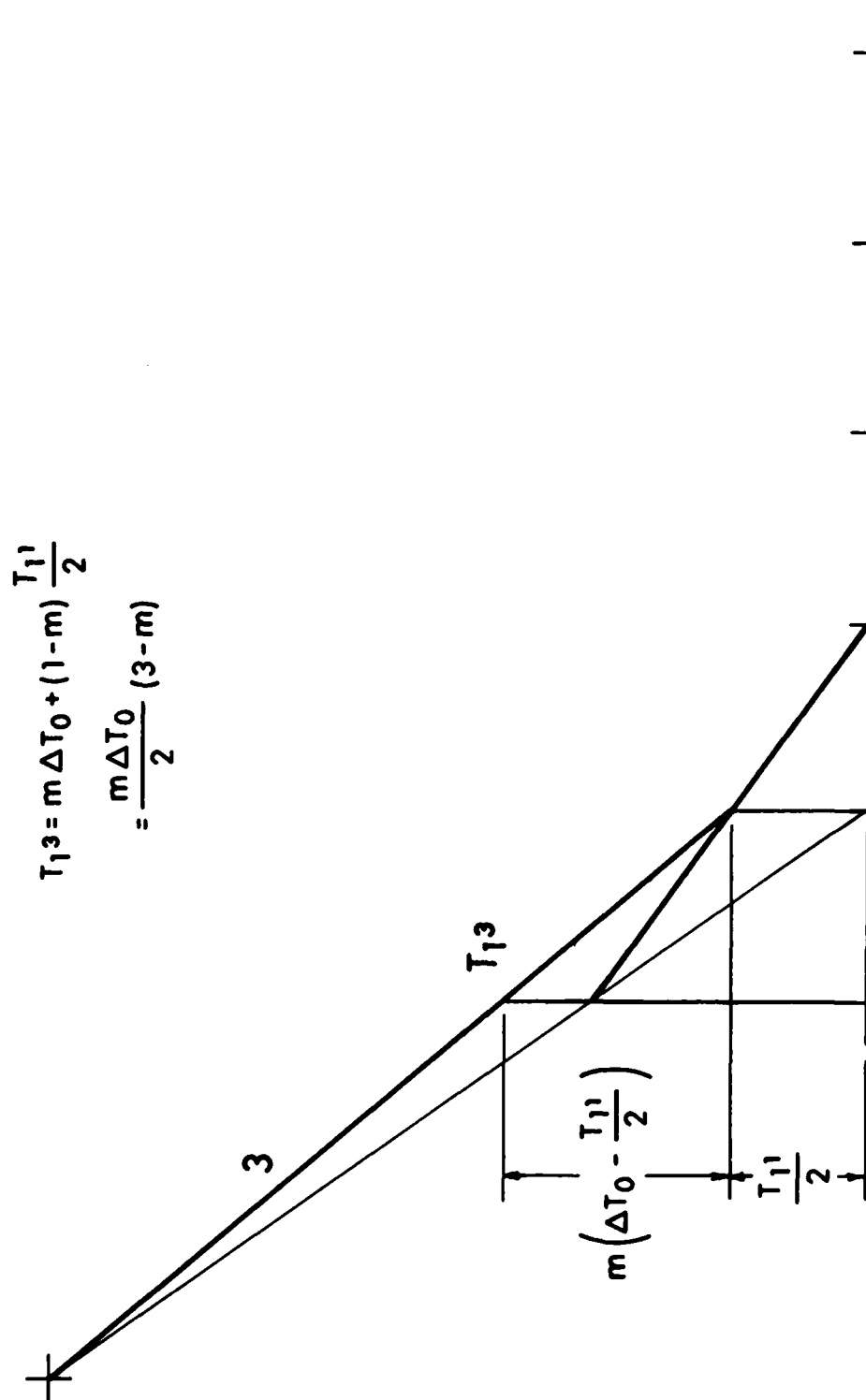


Figure 4. Graphical Determination of T_{13}

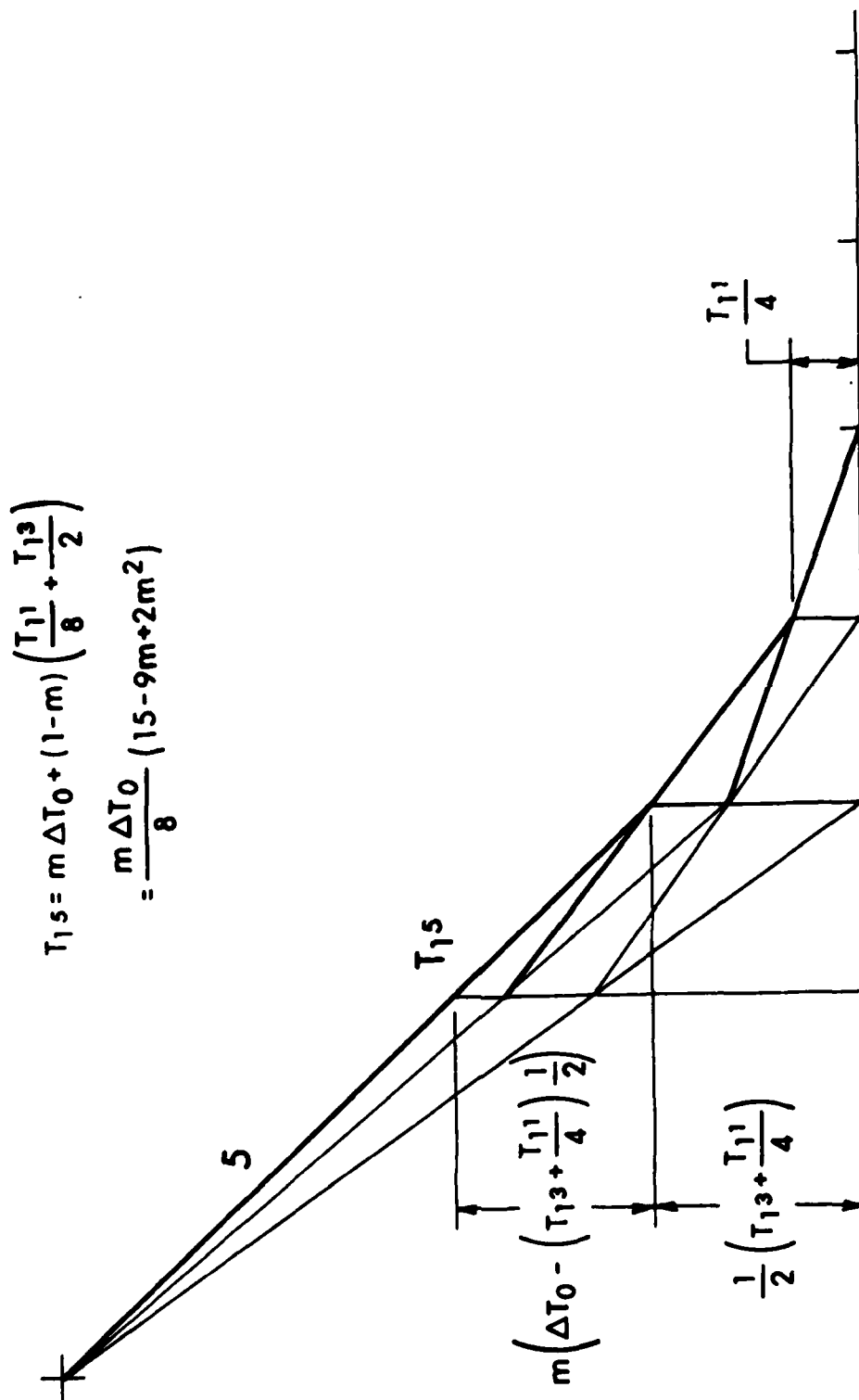


Figure 5. Graphical Determination of T_{15}

$$T_{17} = m\Delta T_0 + (1-m) \left(\frac{T_{11}}{32} + \frac{1}{8} \left(T_{13} + \frac{T_{11}}{4} \right) + \frac{T_{15}}{2} \right)$$

$$= \frac{m\Delta T_0}{16} (35 - 29m + 12m^2 - 2m^3)$$

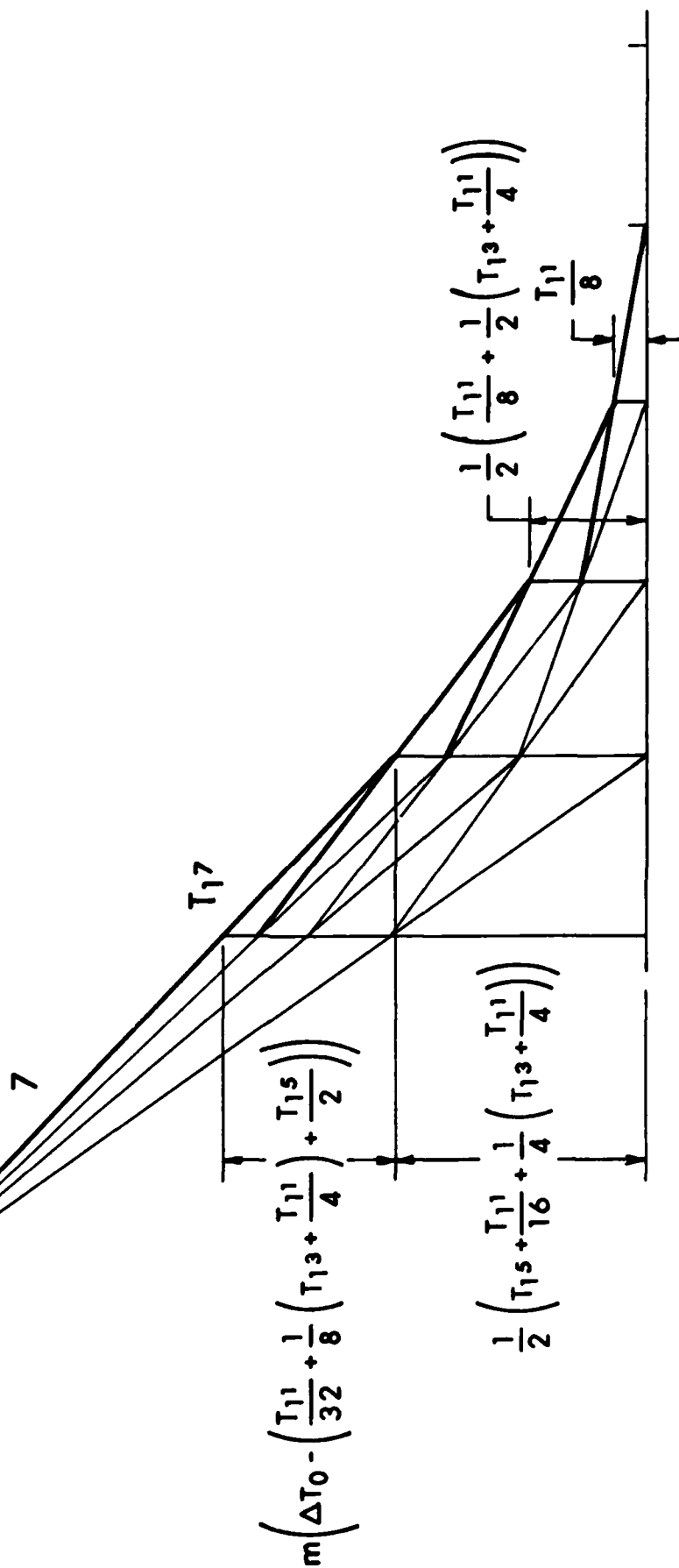


Figure 6. Graphical Determination of T_{17}

$$T_{19} = m\Delta T_0 + (1-m) \left(\frac{5}{128} T_{11} + \frac{T_{13}}{16} + \frac{T_{15}}{8} + \frac{T_{17}}{2} \right)$$

$$= \frac{m\Delta T_0}{128} (315 - 325m + 190m^2 - 60m^3 + 8m^4)$$

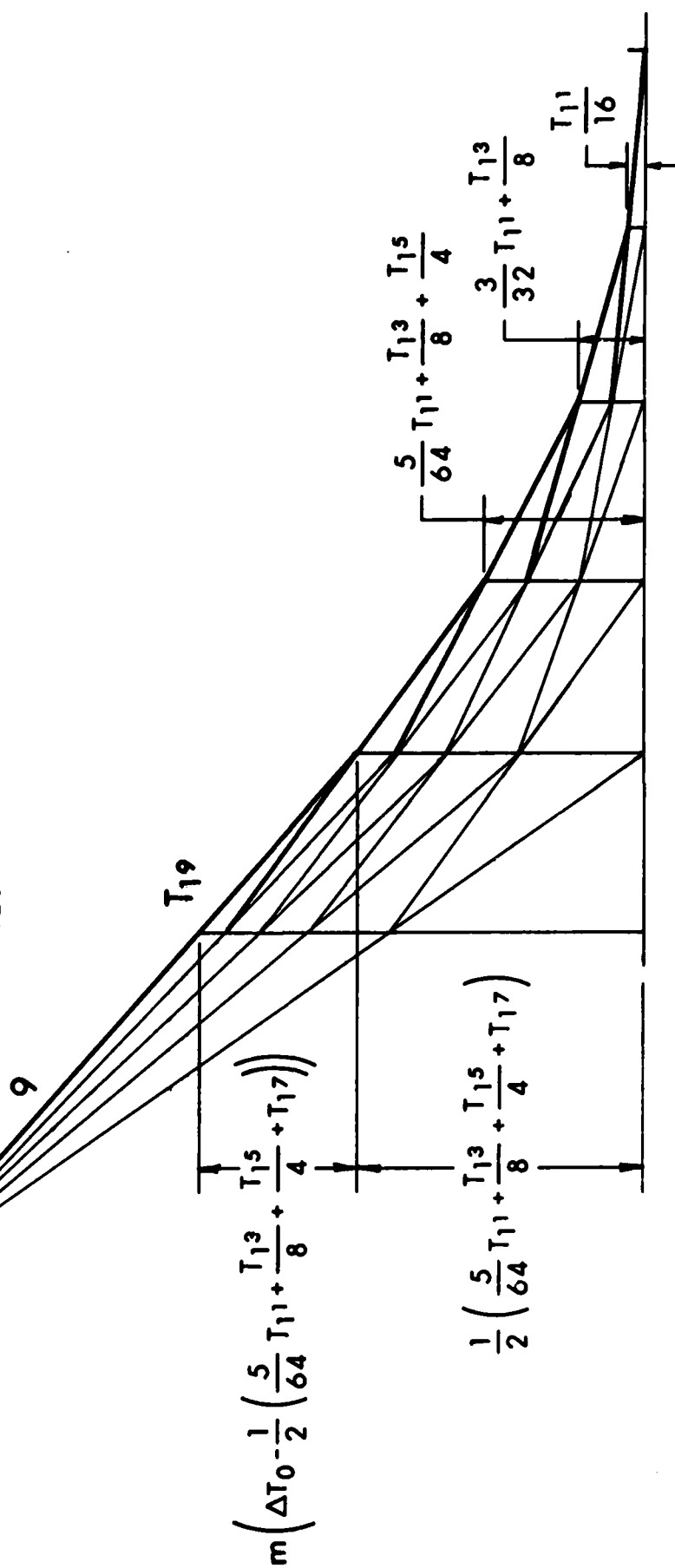


Figure 7. Graphical Determination of T_{19}

TABLE 1. ALGEBRAIC SPECIFICATION OF T_{1n}

$$T_{10} = T_{n0}$$

$$T_{11} = T_{12} = m \Delta T_0 + T_{10} = m \Delta T_0 \phi_1 + T_{10}$$

$$T_{13} = T_{14} = \frac{1}{2} m \Delta T_0 (3-m) + T_{10} = m \Delta T_0 \phi_3 + T_{10}$$

$$T_{15} = T_{16} = \frac{1}{4} m \Delta T_0 (7.5-4.5m + m^2) + T_{10} = m \Delta T_0 \phi_5 + T_{10}$$

$$T_{17} = T_{18} = \frac{1}{8} m \Delta T_0 (17.5-14.5m + 6m^2 - m^3) + T_{10} = m \Delta T_0 \phi_7 + T_{10}$$

$$T_{19} - T_{10} = \frac{1}{16} m \Delta T_0 (39.375-40.625m + 23.75m^2 - 7.5m^3 + m^4) + T_{10} = m \Delta T_0 \phi_9 + T_{10}$$

where ϕ_n is as defined above.

TABLE 2. ALGEBRAIC SPECIFICATION OF T_{2n}

$$T_{20} = T_{21}$$

$$T_{22} = T_{23} = \frac{1}{2} m \Delta T_0 + T_{20} = m \Delta T_0 \theta_3 + T_{20}$$

$$T_{24} = T_{25} = \frac{1}{4} m \Delta T_0 (3.5-m) + T_{20} = m \Delta T_0 \theta_5 + T_{20}$$

$$T_{26} = T_{27} = \frac{1}{8} m \Delta T_0 (9.5-5m + m^2) + T_{20} = m \Delta T_0 \theta_7 + T_{20}$$

$$T_{28} = T_{29} = \frac{1}{16} m \Delta T_0 (24.25 - 19.75 m + 6.5 m^2 - m^3) + T_{20} = m \Delta T_0 \theta_9 + T_{20}$$

where θ_n is as defined above.

The calculating technique is demonstrated by example, using the HP-97, in Appendix C.

Evaluation of \bar{h} from Experimental Data

If an experimental wall temperature distribution^{1,4} can be established, it is possible to read the temperature rise at any two times and solve the algebraic set of equations of Table 1 to eliminate T_o . The resulting expressions are single valued in "m" and solvable. Using the most convenient divisor,

$$\frac{T_1^3 - T_1^o}{m\Delta T_o \phi_1} = \frac{1}{2} (3-m) = \phi_3(m) , \quad (8)$$

$$\frac{T_1^5 - T_1^o}{m\Delta T_o \phi_1} = \frac{1}{2} (7.5 - 4.5m + m^2) = \phi_5(m) , \quad (9)$$

$$\frac{T_1^7 - T_1^o}{m\Delta T_o \phi_1} = \frac{1}{8} (17.5 - 14.5m + 6m^2 - m^3) = \phi_7(m) , \quad (10)$$

$$\frac{T_1^9 - T_1^o}{m\Delta T_o \phi_1} = \frac{1}{16} (39.375 - 40.625m + 23.75m^2 - 7.5m^3 + m^4) = \phi_9(m) , \quad (11)$$

whereby
$$\frac{T_1^n - T_1^o}{\Delta T_o} = m \phi_n(m) \phi_1 . \quad (12)$$

The solution iterates "m" until the experimental and calculated T_{1n} differ by less than a pre-selected error bound. The heat transfer coefficient, \bar{h} , is then deduced from the definition of "m."

Appendix D contains a sample calculation and printout of the HP-97 program for illustration.

Determination of T_{0n} from Experimental Data

Plainly, the extension of the procedure is to examine the average value of the driving gas temperature over the subintervals, i.e., those within the

elapsed time interval. Using values of T_{11} and T_{13} , the intersection of the rays by the construction of Figure 4 locates the value of T_{0n} for the subinterval between time 1 and time 3. The remaining intersections are similarly determined except for the period between time 0 and time 1. T_{11} is directly determined by the physical constraints of the finite difference equation. Figures 8 through 12 illustrate and Tables 3 and 4, based on the following identities, summarize the procedure. Table 3 considers $m = \text{constant}$ while Table 4 allows a variable m .

$$\frac{T_{11}}{T_{0n}} = m, \quad 0 < t < 1, \quad (13)$$

$$\frac{T_{13} - T_{23}}{T_{0n} - T_{23}} = m, \quad 1 < t < 3, \quad (14)$$

$$\frac{T_{15} - T_{25}}{T_{0n} - T_{25}} = m, \quad 3 < t < 5, \quad (15)$$

$$\frac{T_{17} - T_{27}}{T_{0n} - T_{27}} = m, \quad 5 < t < 7, \quad (16)$$

$$\frac{T_{19} - T_{29}}{T_{0n} - T_{29}} = m, \quad 7 < t < 9. \quad (17)$$

T_{2n} is listed in Table 2 and T_{n0} commonly adds to zero.

For the subinterval temperature rise and a corresponding " m ," the local heat transfer coefficient can be calculated by the methods demonstrated in Appendix D.

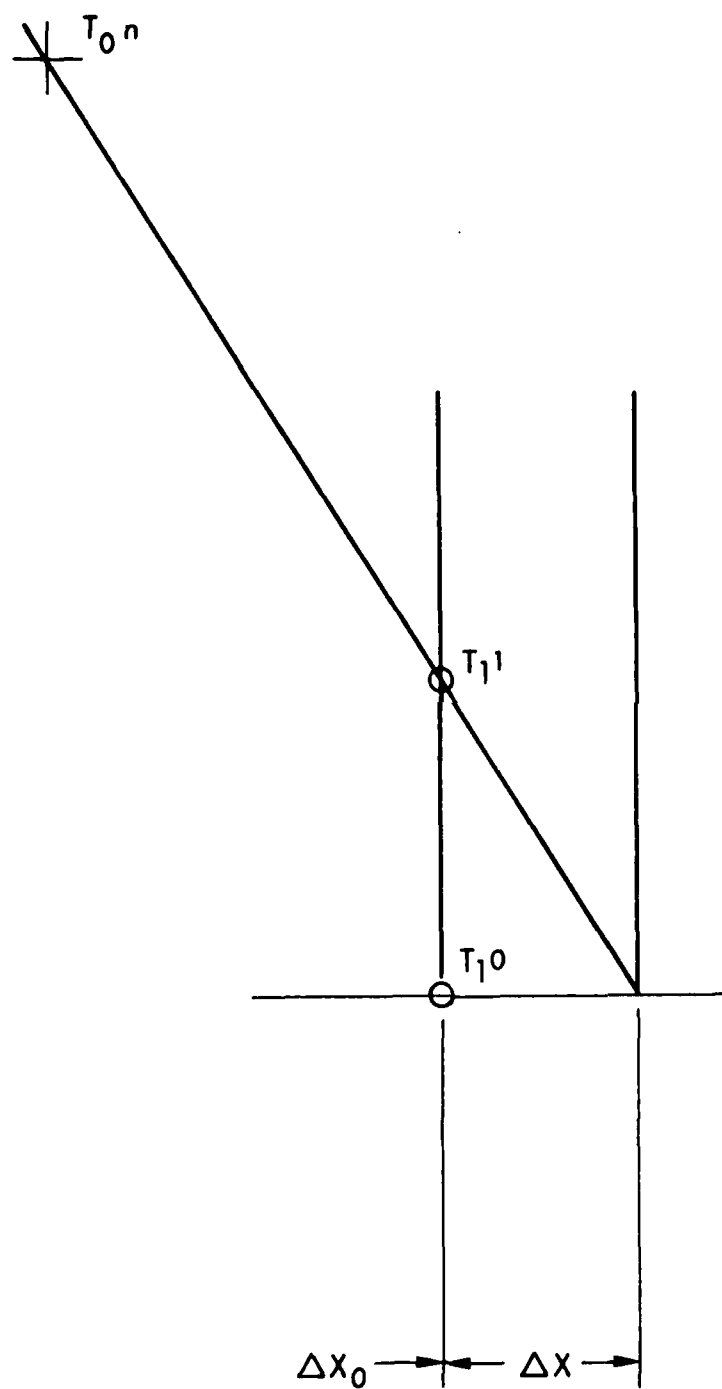


Figure 8. Schmidt Plot for Initial Subinterval from 0 to 1

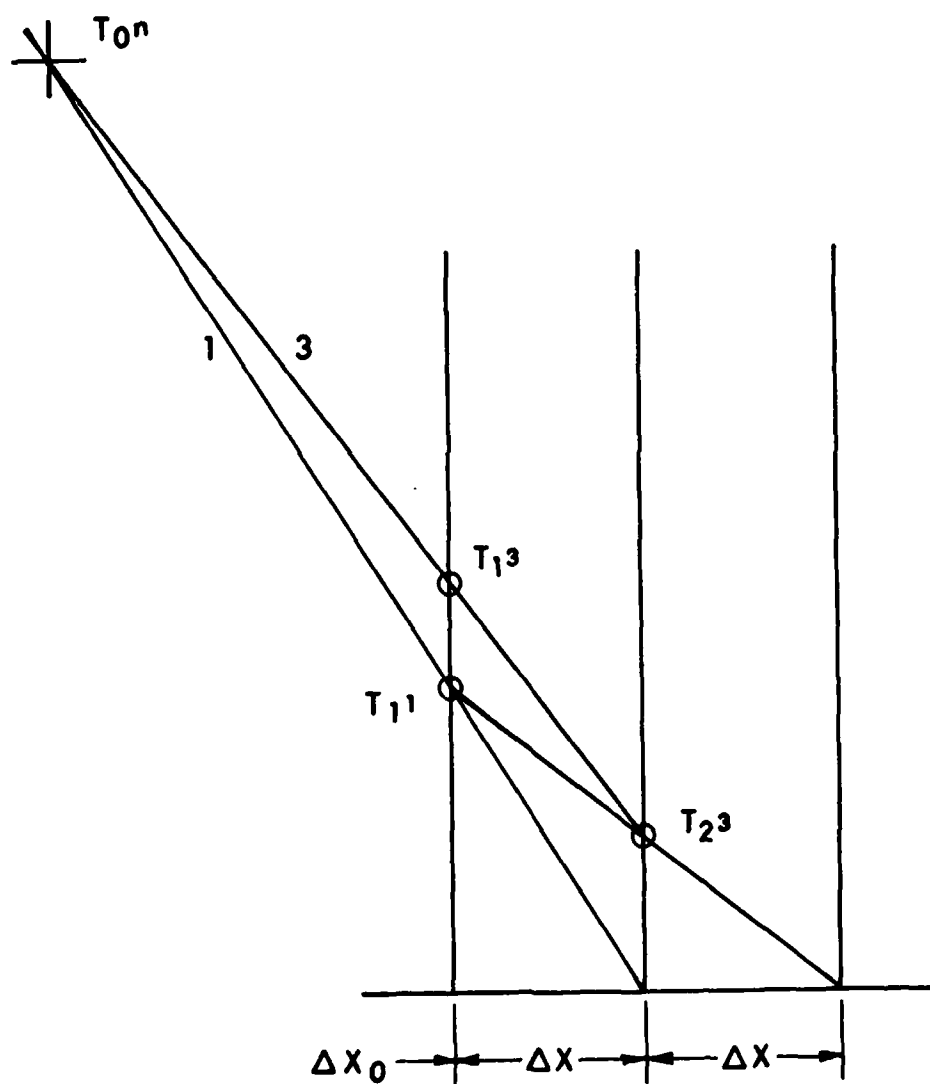


Figure 9. Schmidt Plot for Time Interval from 1 to 3

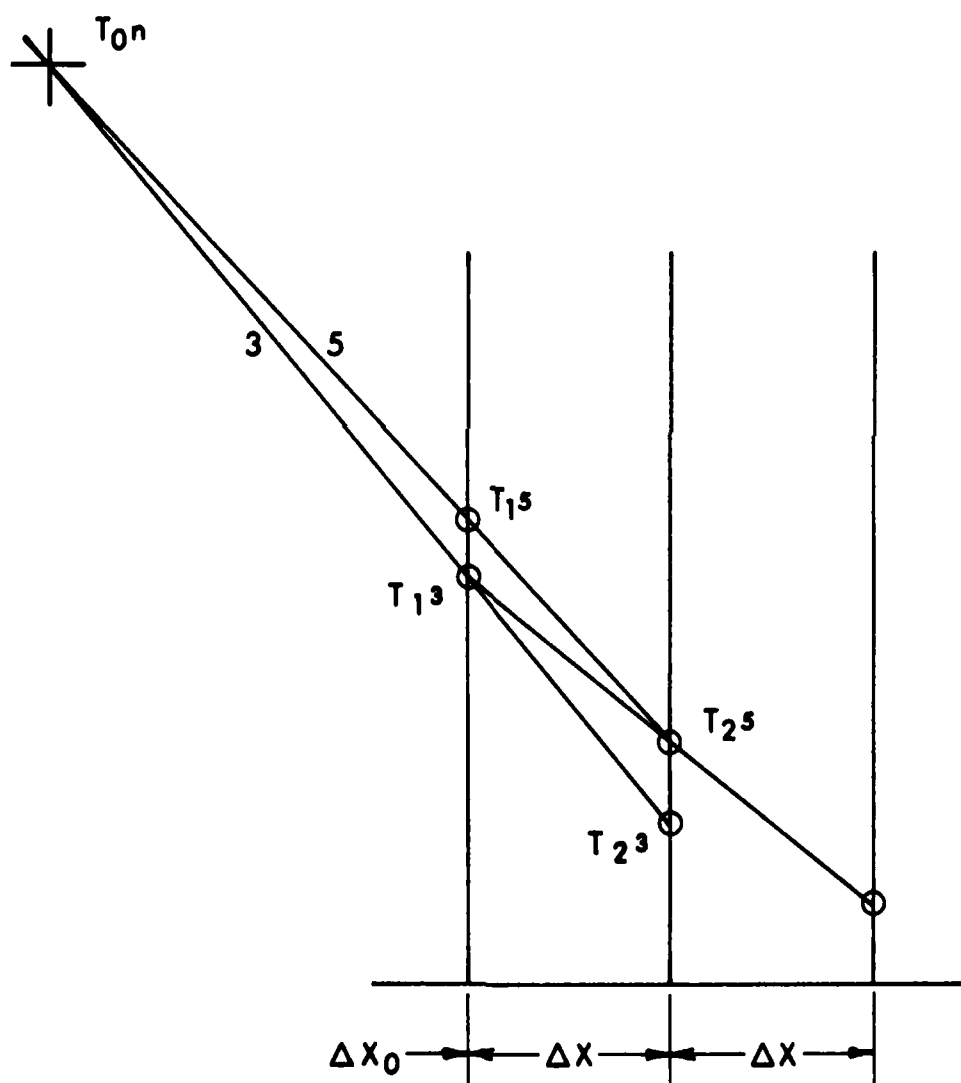


Figure 10. Schmidt Plot for Time Interval from 3 to 5

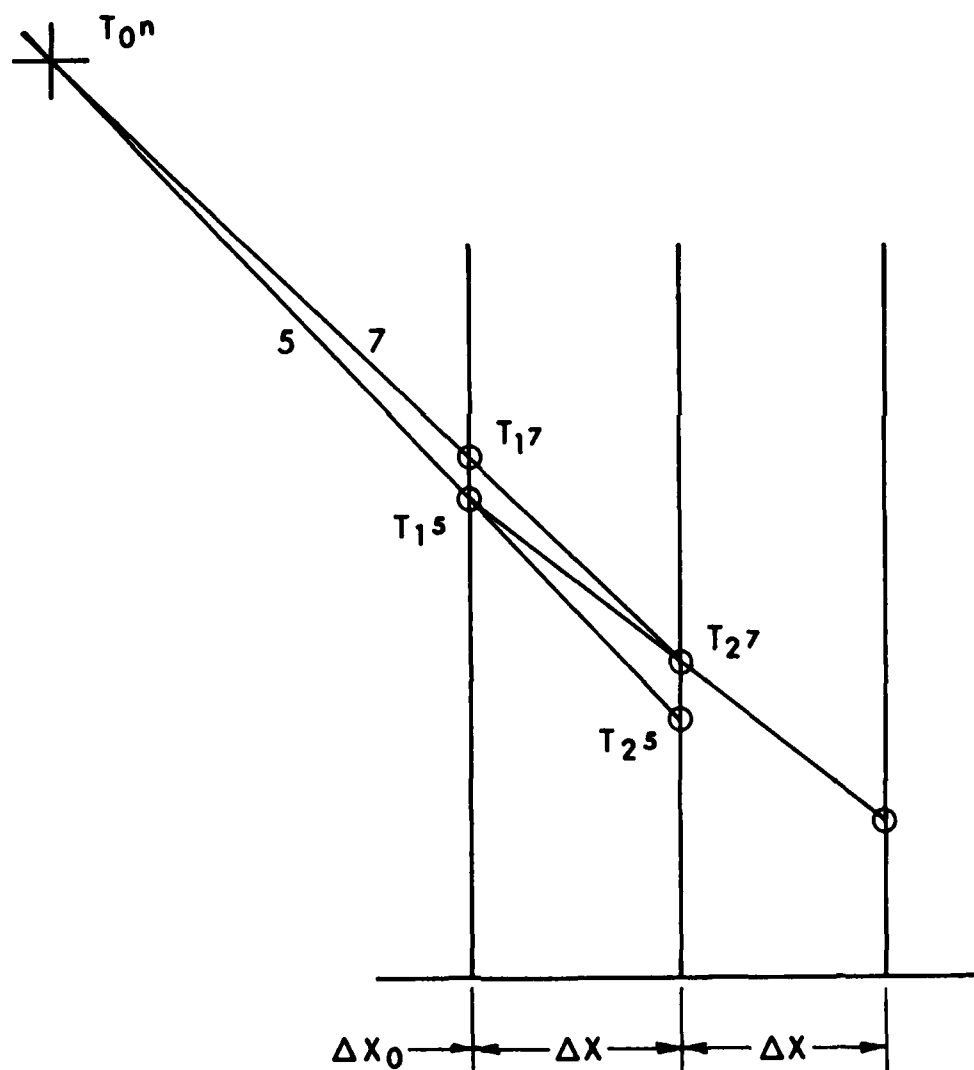


Figure 11. Schmidt Plot for Time Interval from 5 to 7

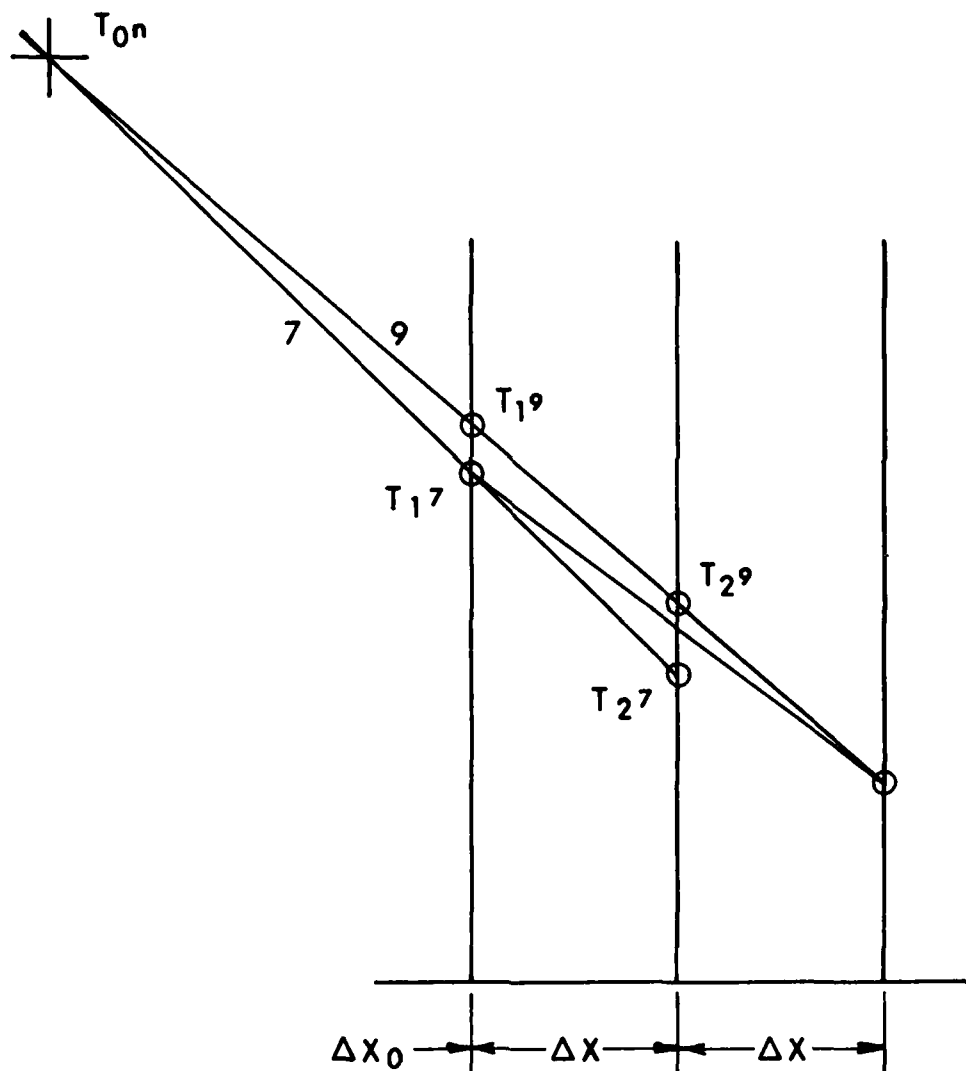


Figure 12. Schmidt Plot for Time Interval from 7 to 9

TABLE 3. ALGEBRAIC SPECIFICATION OF T_{0n} FOR $m = \text{CONSTANT}$

Time Interval		T_{0n}
From	To	For " m " = constant - $\frac{T_1 1}{T_{0n}}$
0	1	$2 T_1 1$
1	3	$\frac{(T_1 1)^2}{3 T_1 1 - 2 T_1 3}$
3	5	$\frac{(T_1 1)^2 + 4 T_1 1 T_1 3}{9 T_1 1 + 4 T_1 3 - 8 T_1 5}$
5	7	$\frac{(T_1 1)^2 + 2 T_1 1 T_1 3 + 8 T_1 1 T_1 5}{17 T_1 1 + 2 T_1 3 + 8 T_1 5 - 16 T_1 7}$
7	9	$\frac{5 (T_1 1)^2 + 8 T_1 1 T_1 3 + 16 T_1 1 T_1 5 + 64 T_1 1 T_1 7}{133 T_1 1 + 8 T_1 3 + 16 T_1 5 + 64 T_1 7 - 128 T_1 9}$

TABLE 4. ALGEBRAIC SPECIFICATION OF T_0^n FOR $n \neq$ CONSTANT

Time Interval		T_0^n
From	To	For "m" variable
0	1	$2 T_1 1$
1	3	$\frac{(T_1 1)^2}{3 T_1 1 - 2 T_1 3}$
3	5	$\frac{4 T_1 1 - 9 T_1 1 T_1 3 - 2 (T_1 3)^2 + 8 T_1 3 T_1 5}{3 T_1 1 - 10 T_1 3 + 8 T_1 5}$
5	7	$\frac{- T_1 1 T_1 5 + 2 T_1 1 T_1 7 - 2 T_1 3 T_1 5 + 8 T_1 3 T_1 7 - 8 (T_1 5)^2}{16 T_1 7 - 16 T_1 5 + T_1 1 + 6 T_1 3 - 8 T_1 5}$
7	9	$\frac{- 5 T_1 1 T_1 7 - 8 T_1 3 T_1 7 - 16 T_1 5 T_1 7 - 64 (T_1 7)^2 + 8 T_1 1 T_1 9 + 16 T_1 3 T_1 9 + 64 T_1 5 T_1 9}{128 T_1 9 - 192 T_1 7 + 3 T_1 1 + 8 T_1 3 + 48 T_1 5}$

III. RESULTS

The data from References 11, 12 is used to examine some of the implications of the equations. Figure 13¹² provides the temperature history of the interior barrel surface of a bench mounted 20 mm weapon firing TB-1 propellant. The thermocouple was located immediately forward of the chamber. For the idealized conditions previously specified, i.e., constant T_o equal to the adiabatic flame temperature of the propellant and univalued \bar{h} and with the properties given in Table D-1, the heat transfer coefficient corresponding to a maximum wall surface temperature rise of 842°F (450°C) is found to be 10,953 B/hr ft²F (1656 cal/hr cm² C). This result is obtained by iterating " m " and $T_{19} - T_{10}$ until the calculated agrees with the experimental temperatures. Figure 14 compares three different driving gas temperatures for the cases of an assumed constant heat transfer coefficient and adiabatic flame temperature source and the alternate cases where the heat transfer coefficient is allowed to vary within the subintervals--in one instance being an averaged constant over the full interval and in the other being coupled to the local effective gas temperature. Figure 15 shows the corresponding heat transfer coefficients for this example.

IV. CONCLUSIONS

With reliable digital temperature recording to one millisecond resolution and current desk top calculating facility, the Schmidt plot approach can be used to establish the effective heat transfer coefficient for experimental data where the transport properties of the system may be assumed constant.

¹¹ Artillery Ammunition Master Calibration Chart, Material Testing Directorate Report 1375, 15th Revision, Aberdeen Proving Ground, MD 1973.

¹² Unpublished Test Data, Interior Ballistics Division, Ballistic Research Laboratory APG, MD 1980.

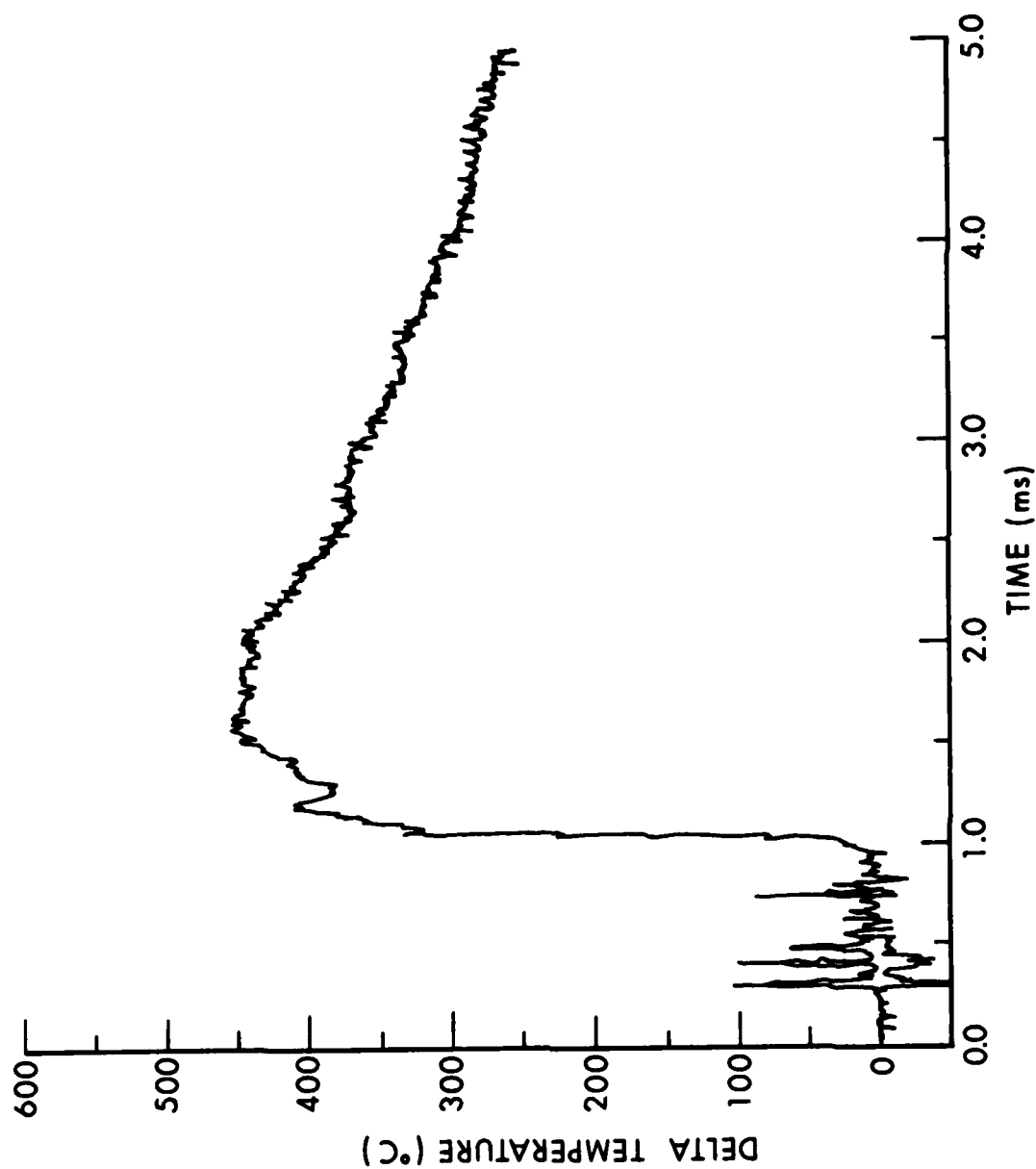


Figure 13. Experimental Wall Temperature History for Special Propellant Round

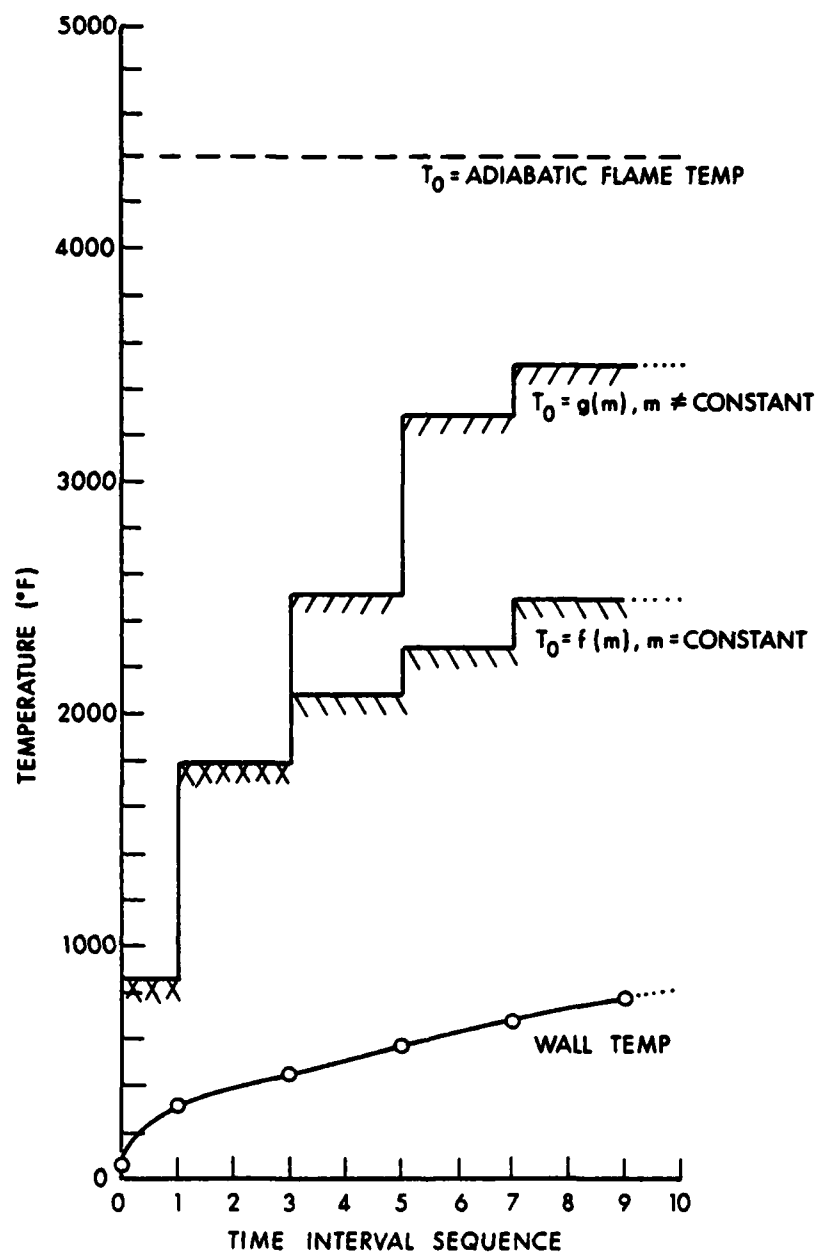


Figure 14. Driving Gas Temperature Profiles

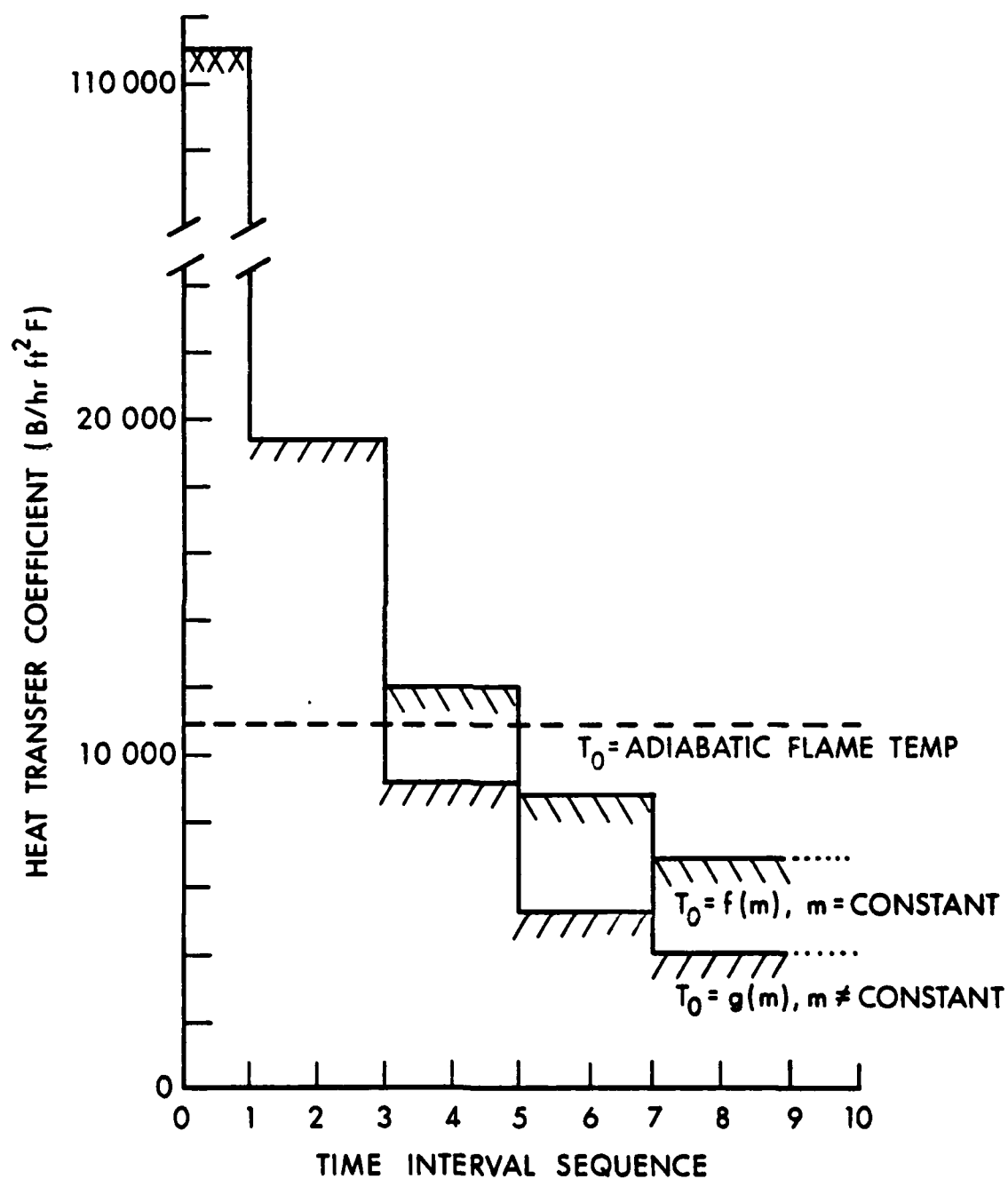


Figure 15. Heat Transfer Coefficient Profiles

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3. Max Jacob, Heat Transfer, Vol. 1, John Wiley and Sons, New York, 1949.
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APPENDIX A

TEMPERATURE GRADIENT IN A TWO DIMENSIONAL PLANE WALL

APPENDIX A

TEMPERATURE GRADIENT IN A TWO DIMENSIONAL PLANE WALL

For the simple geometry represented by a semi-infinite flat plate exposed to a suddenly imposed constant temperature gas on one surface, the Schmidt plot takes the form given on Figure A-1. The initial distance increment, Δx_0 , is made proportional to the film coefficient conductance while the following nine, Δx , characterize the metal. Within the given calculation, the number of distance increments is determined by the storage capacity of the calculator. There is no limit to the number of time cycles.

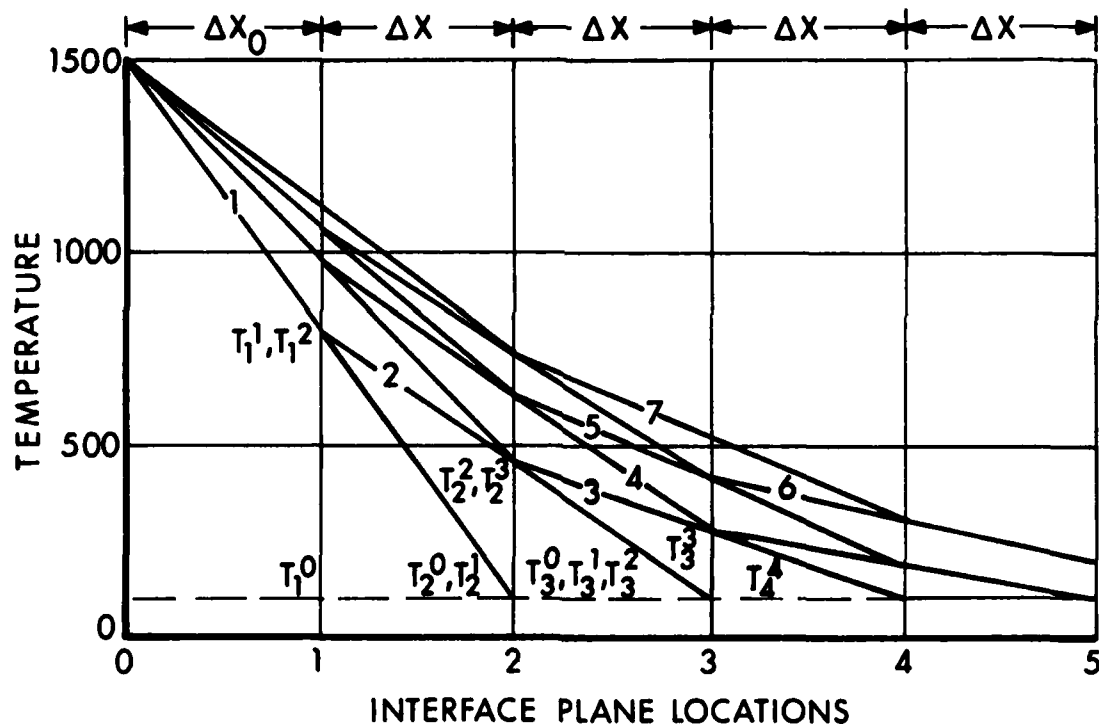


Figure A-1. Schmidt Plot for Schematic Slab Temperature Profile

The problem is to establish the interface time-temperatures in order to insure that the wall material strength criteria is not exceeded. Table A-1, following, illustrates the stepping progression in the finite difference parameters and Figure A-2 presents the results of a specific example.

TABLE A-1. STEPPING PROGRESSION IN TEMPERATURE TIME PARAMETERS FOR SLAB

		TIME PROGRESSION \longrightarrow										
DISTANCE		t^0	t^1	t^2	t^3	t^4	t^5	t^6	t^7	t^8	t^9	t^{10}
FILM \downarrow \uparrow	x_0	T_0	T_{01}	T_{02}	T_{03}	T_{04}	T_{05}	T_{06}	T_{07}	T_{08}	T_{09}	T_{10}
	x_1	T_1	$T_{20+\Delta x} \frac{T_0 - T_{20}}{\Delta x_1 + \Delta x}$	T_{11}	$T_{22+\Delta x} \frac{T_0 - T_{22}}{\Delta x_1 + \Delta x}$	T_{13}	$T_{24+\Delta x} \frac{T_0 - T_{24}}{\Delta x_1 + \Delta x}$	T_{15}	$T_{26+\Delta x} \frac{T_0 - T_{26}}{\Delta x_1 + \Delta x}$	T_{17}	$T_{28+\Delta x} \frac{T_0 - T_{28}}{\Delta x_1 + \Delta x}$	T_{19}
	x_2	T_2	T_{20}	$.5[T_{11} + T_{31}]$	T_{22}	$.5[T_{13} + T_{33}]$	T_{24}	$.5[T_{15} + T_{35}]$	T_{26}	$.5[T_{17} + T_{37}]$	T_{28}	$.5[T_{19} + T_{39}]$
	x_3	T_3	$.5[T_{20} + T_{40}]$	T_{31}	$.5[T_{22} + T_{42}]$	T_{33}	$.5[T_{24} + T_{44}]$	T_{35}	$.5[T_{26} + T_{46}]$	T_{37}	$.5[T_{28} + T_{48}]$	T_{39}
	x_4	T_4	T_{40}	$.5[T_{31} + T_{51}]$	T_{42}	$.5[T_{33} + T_{53}]$	T_{44}	$.5[T_{35} + T_{55}]$	T_{46}	$.5[T_{37} + T_{57}]$	T_{48}	$.5[T_{39} + T_{59}]$
	x_5	T_5	$.5[T_{40} + T_{60}]$	T_{51}	$.5[T_{42} + T_{62}]$	T_{53}	$.5[T_{44} + T_{64}]$	T_{55}	$.5[T_{46} + T_{66}]$	T_{57}	$.5[T_{48} + T_{68}]$	T_{59}
	x_6	T_6	T_{60}	$.5[T_{51} + T_{71}]$	T_{62}	$.5[T_{53} + T_{73}]$	T_{64}	$.5[T_{55} + T_{75}]$	T_{66}	$.5[T_{57} + T_{77}]$	T_{68}	$.5[T_{59} + T_{79}]$
	x_7	T_7	$.5[T_{60} + T_{80}]$	T_{71}	$.5[T_{62} + T_{82}]$	T_{73}	$.5[T_{64} + T_{84}]$	T_{75}	$.5[T_{66} + T_{86}]$	T_{77}	$.5[T_{68} + T_{88}]$	T_{79}
	x_8	T_8	T_{80}	$.5[T_{71} + T_{91}]$	T_{82}	$.5[T_{73} + T_{93}]$	T_{84}	$.5[T_{75} + T_{95}]$	T_{86}	$.5[T_{77} + T_{97}]$	T_{88}	$.5[T_{79} + T_{99}]$
	x_9	T_9	$.5[T_{80} + T_{100}]$	T_{91}	$.5[T_{82} + T_{102}]$	T_{93}	$.5[T_{84} + T_{104}]$	T_{95}	$.5[T_{86} + T_{106}]$	T_{97}	$.5[T_{88} + T_{108}]$	T_{99}
	x_{10}	T_{10}	T_{90}	T_{91}	T_{92}	T_{93}	T_{94}	T_{95}	T_{96}	T_{97}	T_{98}	T_{99}
SLAB \downarrow \uparrow												

There are two branches to the algorithm. One branch describes the conditions at odd-numbered time cycles such that

$$T_1^t = T_2^{t-1} + \frac{\Delta x (T_0 - T_2^{t-1})}{\Delta x + \Delta x_0} \quad (A-1)$$

$$T_2^t = T_2^{t-1} \quad (A-2)$$

$$T_3^t = \frac{T_2^{t-1} + T_4^{t-1}}{2} \quad (A-3)$$

$$T_4^t = T_4^{t-1} \quad (A-4)$$

$$T_5^t = \frac{T_4^{t-1} + T_6^{t-1}}{2} \quad (A-5)$$

$$T_6^t = T_6^{t-1} \quad (A-6)$$

$$T_7^t = \frac{T_6^{t-1} + T_8^{t-1}}{2} \quad (A-7)$$

$$T_8^t = T_8^{t-1} \quad (A-8)$$

$$T_9^t = \frac{T_8^{t-1} + T_{10}^{t-1}}{2} \quad (A-9)$$

$$T_{10}^t = T_9^{t-1} \quad (A-10)$$

The second branch describes conditions at even-numbered time cycles such that

$$T_1^t = T_1^{t-1} \quad (A-11)$$

$$T_2^t = \frac{T_1^{t-1} + T_3^{t-1}}{2} \quad (A-12)$$

$$T_3^t = T_3^{t-1} \quad (A-13)$$

$$T_4^t = \frac{T_3^{t-1} + T_5^{t-1}}{2} \quad (A-14)$$

$$T_5^t = T_5^{t-1} \quad (A-15)$$

$$T_6^t = \frac{T_5^{t-1} + T_7^{t-1}}{2} \quad (A-16)$$

$$T_7^t = T_7^{t-1} \quad (A-17)$$

$$T_8^t = \frac{T_7^{t-1} + T_9^{t-1}}{2} \quad (A-18)$$

$$T_9^t = T_9^{t-1} \quad (A-19)$$

$$T_{10}^t = T_9^{t-1} \quad (A-20)$$

The magnitude of the time cycles is determined from the initial definitions such that

$$\frac{\Delta x^2}{2a\Delta t} = 1 \quad , \quad (A-21)$$

or

$$\Delta t = \frac{\Delta x^2}{2a} \quad ,$$

where

$$a = \frac{k}{\rho c} \quad , \quad (A-22)$$

and k is thermal conductivity,
 c is specific heat, and
 ρ is material density.

Whereby

$$\Delta t = \frac{c\Delta x^2}{2\rho k} \quad (A-23)$$

Example

The calculating technique is demonstrated by example. Assume a semi-infinite steel wall 12 inches (30.2 cm) thick suddenly exposed to a 5000°F (2760°C) gas flow over one face. After a measured interval of 26 sec, the gas temperature is reduced to ambient. Table A-2 defines the initial conditions and operating parameters for the program input. Figure A-2 presents a Schmidt plot of the results. The HP-97 listing follow Figure A-2.

TABLE A-2. DEFINITION OF BOUNDARY CONDITIONS FOR SAMPLE SLAB PROBLEM

	Heat Source	Film	Steel Slab	Reference
Initial Temperature (T_0)	5000 F 2760 C 2730 N	100 F 37.7 C 280 N	100 F 37.7 C 280 N	Assumed
Unit Film Conductance (h)		25 B/hr ft ² F 3.782 cal/hr cm ² C 974.1 CAL ² /hr N		(5)
Thermal Conductivity (k)			10 B/hr ft F 46.11 cal/hr cm C 974.1 CAL ² /hr N	(5)
Diffusivity (α)			.48 ft ² /hr 446 cm ² /hr 5.0 CAL ² /hr	(5)
Equivalent Film Thickness (k/h)		4.8 in 12.19 cm 1.0 CAL		Construction
Slab Thickness			12 in 30.19 cm 2.5 CAL	Assumed ($n = 10$)
Distance Increment (Δx_0) (Δx)		(Δx_0) 4.8 in 12.19 cm 1.0 CAL	(Δx) 1.0 in 2.54 cm .208 CAL	$\Delta x_0 = k/h$
Time Increment (τ)		26.04 sec	26.04 sec	$\Delta \tau_c = n \Delta \tau$ $\Delta \tau = \Delta x^2 / 2 \alpha$

HP-97 INITIAL REGISTER CONTENTS

Registers R_0 through R_9 enter the initial temperatures at the interstitial planes.

R_A indicates the number of time cycles required to elapse 2.6 minutes (for this example).

R_B gives the distance increment for the steel.

R_C gives the sum of the steel and equivalent film increments.

R_D and R_E indicate the initial temperature at the terminal plane.

R_I enters the number of time increments completed (usually 0).

R_{S0} gives the effective ambient temperature of the gas during the cooling.

OUTPUT

The printed output presents the temperature in the enumerated sequence of the interstitial planes. The terminal plane temperature is given in the D register and the number of time cycles completed in the I register. The real time elapsed is this number times the time interval.

SAMPLE INPUT AND OUTPUT

The program entry employed with the HP-97 is given below. Any consistant system of units is suitable.

Primary Registers	Initial Values	Example
R ₀	T ₀	2730 N
R ₁	T ₁	280 N
R ₂	T ₂	280 N
R ₃	T ₃	280 N
R ₄	T ₄	280 N
R ₅	T ₅	280 N
R ₆	T ₆	280 N
R ₇	T ₇	280 N
R ₈	T ₈	280 N
R ₉	T ₉	280 N
R _A	Y	6
R _B	Δx	.208 CAL
R _C	$\Delta x_0 + \Delta x$	1.208 CAL
R _D	T ₁₀	208 N
R _E	T ₁₀	280 N
R _I	0	0

Secondary Registers

R ₀	T _{AMBIENT}	280 N
----------------	----------------------	-------

Output after 15 time cycles

T ₀	280 N
T ₁	436 N
T ₂	469 N
T ₃	455 N
T ₄	440 N
T ₅	404 N
T ₆	367 N
T ₇	339 N

T ₈	312 N
T ₉	303 N
Intermediate Result	303 N
Intermediate Result	
Intermediate Result	
T ₁₀	294 N
Intermediate Result	
Number of time cycles completed	15

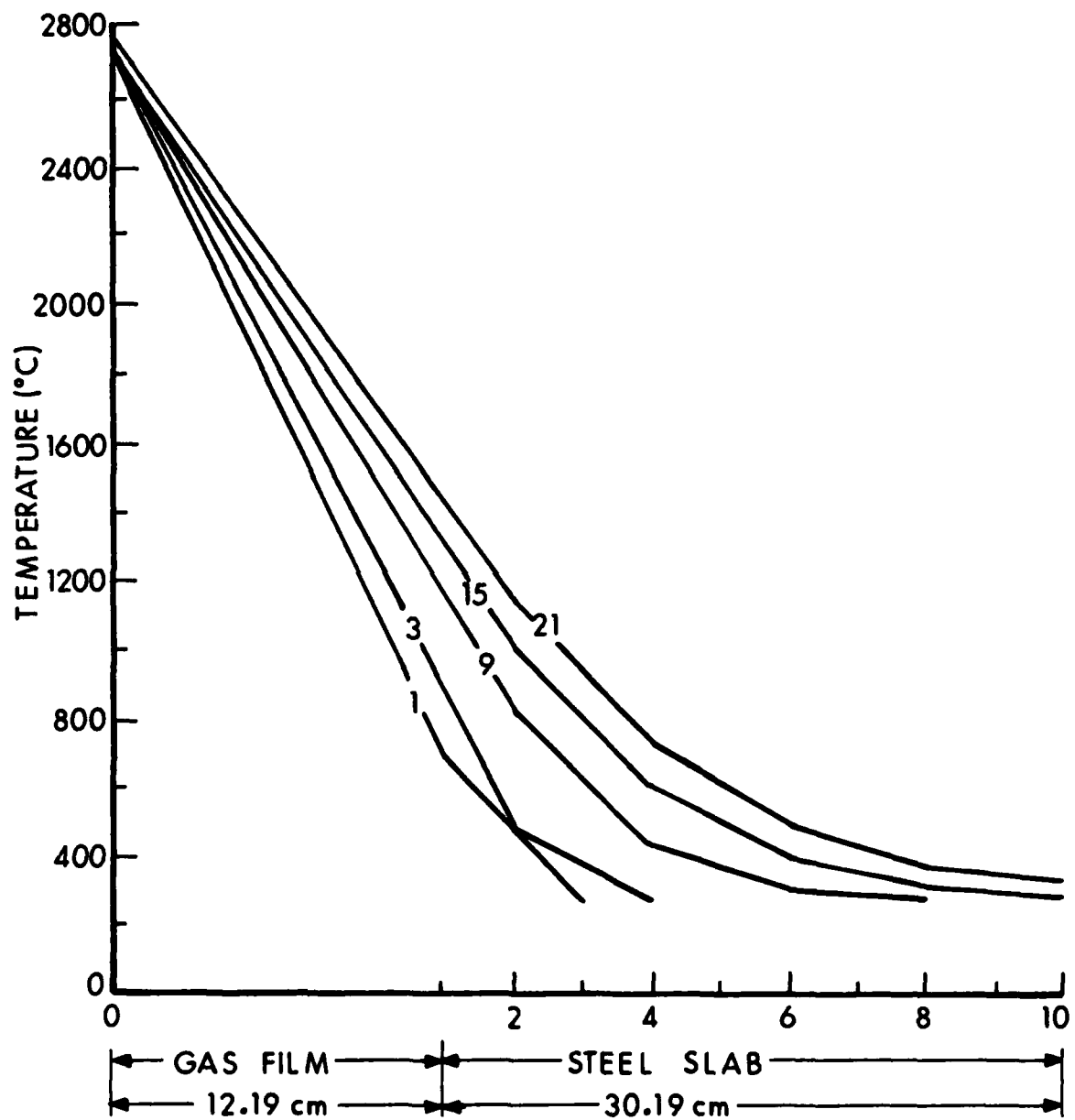


Figure A-2. Schmidt Plot for Sample Slab Problem

PROGRAM LISTING

001	*LBLB	21 12
002	PREG	16-13
003	*LBLA	21 11
004	RCL0	36 00
005	RCL2	36 02
006	-	-45
007	RCLC	36 13
008	÷	-34
009	RCLB	36 12
010	x	-35
011	RCL2	36 02
012	+	-55
013	ST01	35 01
014	CLX	-51
015	RCL2	36 02
016	RCL4	36 04
017	+	-55
018	2	02
019	÷	-24
020	ST03	35 03
021	CLX	-51
022	RCL4	36 04
023	RCL6	36 06
024	+	-55
025	2	02
026	÷	-24
027	ST05	35 05
028	CLX	-51
029	RCL6	36 06
030	RCL8	36 08
031	+	-55
032	2	02
033	÷	-24
034	ST07	35 07
035	CLX	-51
036	RCL8	36 08
037	RCL0	36 10
038	ST0D	35 14
039	+	-55
040	2	02
041	÷	-24
042	ST09	35 09
043	ST0E	35 15
044	CLX	-51
045	ISZI	16 26 46
046	SPC	16-11
047	PREG	16-13
048	*LBLC	21 13
049	RCL1	36 01
050	RCL3	36 03
051	+	-55
052	2	02
053	÷	-24
054	ST02	35 02
055	CLX	-51
056	RCL3	36 03
057	RCL5	36 05
058	+	-55
059	2	02
060	÷	-24
061	ST04	35 04
062	CLX	-51
063	RCL5	36 05
064	RCL7	36 07
065	+	-55
066	2	02
067	÷	-24
068	ST06	35 06
069	CLX	-51
070	RCL7	36 07
071	RCL9	36 09
072	+	-55
073	2	02
074	÷	-24
075	ST08	35 08
076	CLX	-51
077	ISZI	16 26 46
078	RCL1	36 01
079	RCLA	36 11
080	X&Y?	16-35
081	GT0D	22 14
082	GT0A	22 11
083	*LBLD	21 14
084	P&S	16-51
085	RCL0	36 00
086	P&S	16-51
087	ST00	35 00
088	GT0A	22 11
089	R/S	51

APPENDIX B

TEMPERATURE GRADIENT IN A LONG THICK WALLED CYLINDER

APPENDIX B

TEMPERATURE GRADIENT IN A LONG THICK WALLED CYLINDER

In cylindrical coordinates the suddenly imposed temperature is shown in Schmidt plot presentation as Figure B-1, which is a transformation from the physical plane to that of the operating parameters. From the equations of II-A, the transformed equivalent film distance is equal to $\frac{k}{rh}$ for equal radial increments transposed to logarithmically spaced increments in Δj .

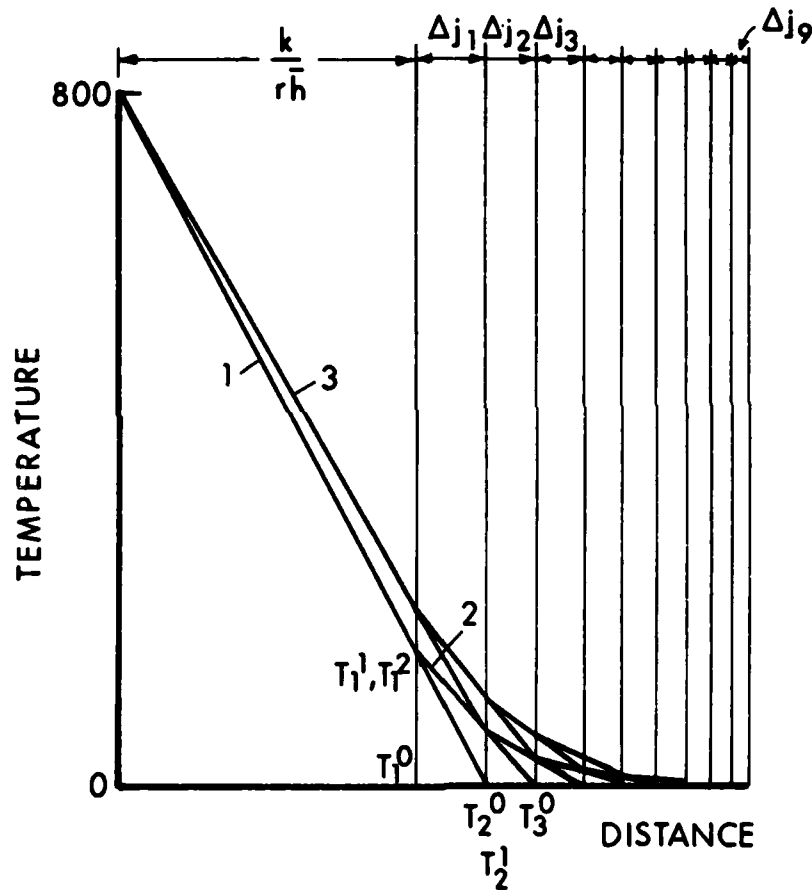


Figure B-1. Schmidt Plot Schematic for Cylindrical Wall Temperature Profile

The problem is that of the slab to establish the time-temperature distance gradient. Table B-1 illustrates the stepping procedure in finite difference parameters, and Figure B-1 plots the results of a specific example.

The odd-numbered time cycles are described by

$$T_1^t = T_2^{t-1} + \left[T_0 - T_2^{t-1} \right] \left[\frac{\Delta j_1}{1 + \Delta j_1} \right] \quad (B-1)$$

$$T_2^t = T_2^{t-1} \quad (B-2)$$

$$T_3^t = T_4^{t-1} + \left[T_2^{t-1} - T_4^{t-1} \right] \left[\frac{\Delta j_3}{\Delta j_2 + \Delta j_3} \right] \quad (B-3)$$

$$T_4^t = T_4^{t-1} \quad (B-4)$$

$$T_5^t = T_6^{t-1} + \left[T_4^{t-1} - T_6^{t-1} \right] \left[\frac{\Delta j_5}{\Delta j_4 + \Delta j_5} \right] \quad (B-5)$$

$$T_6^t = T_6^{t-1} \quad (B-6)$$

$$T_7^t = T_8^{t-1} + \left[T_6^{n-1} - T_8^{n-1} \right] \left[\frac{\Delta j_7}{\Delta j_6 + \Delta j_7} \right] \quad (B-7)$$

$$T_8^t = T_8^{t-1} \quad (B-8)$$

$$T_9^t = T_{10}^{t-1} + \left[T_8^{n-1} - T_{10}^{n-1} \right] \left[\frac{\Delta j_9}{\Delta j_8 + \Delta j_9} \right] \quad (B-9)$$

$$T_{10}^t = T_9^{t-1} \quad (B-10)$$

The even-numbered time cycles are described by

$$T_1^t = T_1^{t-1} \quad (B-11)$$

$$T_2^t = T_3^{t-1} + \left[T_1^{t-1} - T_3^{t-1} \right] \left[\frac{\Delta j_2}{\Delta j_1 + \Delta j_2} \right] \quad (B-12)$$

$$T_3^t = T_3^{t-1} \quad (B-13)$$

$$T_4^t = T_5^{t-1} + \left[T_3^{t-1} - T_5^{t-1} \right] \left[\frac{\Delta j_4}{\Delta j_3 + \Delta j_4} \right] \quad (B-14)$$

$$T_5^t = T_5^{t-1} \quad (B-15)$$

$$T_6^t = T_7^{t-1} + \left[T_5^{t-1} - T_7^{t-1} \right] \left[\frac{\Delta j_6}{\Delta j_5 + \Delta j_6} \right] \quad (B-16)$$

$$T_7^t = T_7^{t-1} \quad (B-17)$$

$$T_8^t = T_9^{t-1} + \left[T_7^{t-1} - T_9^{t-1} \right] \left[\frac{\Delta j_8}{\Delta j_7 + \Delta j_8} \right] \quad (B-17)$$

$$T_9^t = T_9^{t-1} \quad (B-19)$$

A fixed time increment is found such that

$$\Delta t = \frac{\Delta r^2}{2a}$$

The calculating technique is demonstrated by example. Assume an infinitely long stainless steel cylinder 1.0 inches (2.54 cm) inside diameter and 2.5 inches (6.35 cm) outside diameter suddenly exposed to a constant high temperature gas flow through the bore for 1.31 sec. The properties of the materials and the critical transport properties are given in Table B-2 with the HP-97 listing immediately following.

TABLE B-2. DEFINITION OF BOUNDARY CONDITIONS FOR SAMPLE CYLINDER PROBLEM

	Heat Source	Film	Steel Tube	Reference
Initial Temperature (T_0)	300 F 149 C 380 N	100 F 37.7 C 280 N	100 F 37.7 C 280 N	Assumed
Unit Film Conductance (\bar{h})		250 B/hr ft ² F 37.82 cal/hr cm C 8.84x10 ⁵ CAL ² /hr N		(5)
Thermal Conductivity (k)			10.5 B/hr ft F 48.4 cal/hr cm C 8.84x10 ⁵ CAL ² /hr N	(5)
Diffusivity (a)			.197 ft ² /hr 183 cm ² /hr 4.69 CAL ² /hr	(5)
Equivalent Film Thickness ($k/r_i \bar{h}$)		1.008 ft 30.724 cm 1.0 CAL		Calculation
Maximum Wall Penetration			.038 ft 1.158 cm .038 CAL	$n\Delta r$ ($n = 10$)
Distance Increment (Δr_0) (Δr)		(Δr_0) 1.008 ft 30.724 cm 1.0 CAL	(Δr) .0038 ft .1154 cm .0038 CAL	$\Delta r_0 = k/r_i \bar{h} \Delta t_e^{1/2}$ $\Delta r = (2 a \frac{\Delta t_e}{n})^{1/2}$
Time Increment (Δt) _e		1.31 sec	1.31 sec	Assumed

HP-97 REGISTER CONTENTS

The geometric radial boundaries are specified and equal radial increments are automatically converted to logarithmic parameters within the program. The corresponding initial temperatures must be entered as well as an elapsed time span.

Registers R_{S0} through R_{S9} enter the initial temperatures at the radial interstitial planes.

R_A indicates the number of time cycles required to elapse seconds (for this example).

R_B gives the inner radius.

R_C gives the outer radius.

R_D indicates the effective ambient temperature of the gas during the cooling phase.

R_E enters the initial temperature of the terminal plane.

R_I is given the number 1 for the initial calculation. The program automatically converts this figure to that of the number of time cycles completed at any stage in the calculation.

Note that the program starts with the secondary register filled and the primary register open.

OUTPUT

The printed output presents the temperature in the enumerated sequence of the radial interstitial planes. The terminal plane temperature is given in the D register and the number of time cycles completed in the I register. The real time elapsed is this number times the time interval.

The program entry employed with the HP-97 is given below. Any consistant system of units is suitable.

Primary Registers	Initial Values	Example
R ₀	T ₀	380 N
R ₁	T ₁	280 N
R ₂	T ₂	280 N
R ₃	T ₃	280 N
R ₄	T ₄	280 N
R ₅	T ₅	280 N
R ₆	T ₆	280 N
R ₇	T ₇	280 N
R ₈	T ₈	280 N
R ₉	T ₉	280 N
R _A	Y	3
R _B	r _{inner}	.5
R _C	r _{outer}	2.25
R _D	T _{ambient}	125 N
R _E	T ₁₀	280 N
R _I	1	1

All primary registers are 0.

OUTPUT AFTER 6 TIME CYCLES

T ₀	125 N
T ₁	255 N
T ₂	274 N
T ₃	289 N
T ₄	284 N
T ₅	281 N
T ₆	280 N
T ₇	280 N
T ₈	280 N
T ₉	280 N
Intermediate Result	
Intermediate Result	
Intermediate Result	
T ₁₀	280 N
Numer of time cycles completed	

PROGRAM LISTING

001	*L6LD	21 14
002	RCLB	36 12
003	9	09
004	X	-35
005	ST08	35 08
006	RCLC	36 13
007	RCLB	36 12
008	-	-45
009	RCL0	36 00
010	÷	-24
011	1/X	52
012	.	-62
013	5	05
014	-	-45
015	ST09	35 09
016	RCLI	36 46
017	+	-55
018	1/X	52
019	ST01	35 01
020	ISZI	16 26 46
021	RCL9	36 09
022	RCLI	36 46
023	+	-55
024	1/X	52
025	ST02	35 02
026	ISZI	16 26 46
027	RCLI	36 46
028	RCL9	36 09
029	+	-55
030	1/X	52
031	ST03	35 03
032	ISZI	16 26 46
033	RCLI	36 46
034	RCL9	36 09
035	+	-55
036	1/X	52
037	ST04	35 04
038	ISZI	16 26 46
039	RCLI	36 46
040	RCL9	36 09
041	+	-55
042	1/X	52
043	ST05	35 05
044	ISZI	16 26 46
045	RCLI	36 46
046	RCL9	36 09
047	+	-55
048	1/X	52
049	ST06	35 06
050	ISZI	16 26 46
051	RCLI	36 46
052	RCL9	36 09
053	+	-55
054	1/X	52
055	ST07	35 07
056	ISZI	16 26 46
057	RCLI	36 46
058	RCL9	36 09
059	+	-55
060	1/X	52
061	ST08	35 08
062	ISZI	16 26 46
063	RCLI	36 46
064	RCL9	36 09
065	+	-55
066	1/X	52
067	ST09	35 09
068	0	00
069	ST01	35 01
070	RCLD	36 14
071	ST00	35 00
072	GT08	22 12
073	F2S	16-51
074	*L6LB	21 12
075	F2S	16-51
076	RCL0	36 00
077	RCL2	36 02
078	-	-45
079	F2S	16-51
080	RCL1	36 01
081	F2S	16-51
082	1/X	52
083	1	01
084	+	-55
085	÷	-24

130	+	-55
131	ST07	35 07
132	RCL8	36 08
133	RCL6	36 15
134	-	-45
135	P2S	16-51
136	RCL8	36 08
137	RCL9	36 09
138	÷	-24
139	1	01
140	+	-55
141	P2S	16-51
142	÷	-24
143	RCL6	36 15
144	ST00	35 14
145	+	-55
146	ST09	35 09
147	ST0E	35 15
148	ISZI	16 26 46
149	PREG	16-13
150	RCL1	36 01
151	RCL3	36 03
152	-	-45
153	P2S	16-51
154	RCL1	36 01
155	RCL2	36 02
156	÷	-24
157	1	01
158	+	-55
159	P2S	16-51
160	÷	-24
161	RCL3	36 03
162	+	-55
163	ST02	35 02
164	RCL3	36 03
165	RCL5	36 05
166	-	-45
167	P2S	16-51
168	RCL3	36 03
169	RCL4	36 04
170	÷	-24
171	1	01
172	+	-55
173	P2S	16-51

086	RCL2	36 02
087	+	-55
088	ST01	35 01
089	CLX	-51
090	RCL2	36 02
091	RCL4	36 04
092	-	-45
093	P2S	16-51
094	RCL2	36 02
095	RCL3	36 03
096	÷	-24
097	1	01
098	+	-55
099	P2S	16-51
100	÷	-24
101	RCL4	36 04
102	+	-55
103	ST03	35 03
104	RCL4	36 04
105	RCL6	36 06
106	-	-45
107	P2S	16-51
108	RCL4	36 04
109	RCL5	36 05
110	÷	-24
111	1	01
112	+	-55
113	P2S	16-51
114	÷	-24
115	RCL6	36 06
116	+	-55
117	ST05	35 05
118	RCL6	36 06
119	RCL8	36 08
120	-	-45
121	P2S	16-51
122	RCL6	36 06
123	RCL7	36 07
124	÷	-24
125	1	01
126	+	-55
127	P2S	16-51
128	÷	-24
129	RCL8	36 08

174	÷	-24
175	RCL5	36 05
176	+	-55
177	ST04	35 04
178	RCL5	36 05
179	RCL7	36 07
180	-	-45
181	P2S	16-51
182	RCL5	36 05
183	RCL6	36 06
184	÷	-24
185	1	01
186	+	-55
187	P2S	16-51
188	÷	-24
189	RCL7	36 07
190	+	-55
191	ST06	35 06
192	RCL7	36 07
193	RCL9	36 09
194	-	-45
195	P2S	16-51
196	RCL7	36 07
197	RCL8	36 08
198	÷	-24
199	1	01
200	+	-55
201	P2S	16-51
202	÷	-24
203	RCL9	36 09
204	+	-55
205	ST08	35 08
206	ISZI	16 26 46
207	P2S	16-51
208	RCL1	36 01
209	RCL4	36 04
210	X>Y?	16-34
211	GT0B	22 12
212	RCL0	36 00
213	P2S	16-51
214	ST00	35 00
215	P2S	16-51
216	GT0B	22 12

APPENDIX C
PLANE WALL SURFACE TEMPERATURE

APPENDIX C

PLANE WALL SURFACE TEMPERATURE

Under the idealized conditions as previously specified, the wall temperature progression is established by algebraic determination as expressed in Table 1. For example, assuming an adiabatic flame temperature of M-2 propellant as the driving gas medium, and estimating the time required for the projectile to clear the barrel as .003 sec, and a heat transfer coefficient of 1845 B/hr ft² F, with the physicals as given in Table C-1, the wall temperature at the five time intervals can be read directly from the printout. The complete HP-97 listing follows on p.

INITIAL REGISTER CONTENTS

This program requires a constant driving gas temperature T_o , an initial wall temperature, the thermal conductance and diffusivity of the wall material, and a convective heat transfer coefficient corresponding to an assumed elapsed time increment. It presumes a slab wall and calculates the wall temperature growth from an initial slab depth of approximately .040 in (1 mm).

R_A indicates the driving gas temperature, T_o .

R_B gives the initial ambient temperature, T_n .

R_1 is the elapsed time in hours.

R_2 enters 10, the number of time increments for this example.

R_3 is the average convective heat transfer coefficient over this range.

R_4 gives the metal thermal conductivity.

R_5 is the metal thermal diffusivity.

OUTPUT

The printed output gives the wall temperature for ten sequential increments of time over the elapsed time interval.

TABLE C-1. DEFINITION OF BOUNDARY CONDITIONS FOR SAMPLE PLANE WALL PROBLEM

	Heat Source	Film	Steel Slab	Reference
Initial Temperature (T_0)	5596 F 3091 C 3028 N	70 F 21 C 265 N	70 F 21 C 265 N	(12)
Unit Film Conductance (\bar{h})		1845 B/hr ft ² F 279 cal/hr cm ² C 1.53x10 ⁸ CAL ² /hr N		(5)
Thermal Conductivity (k)			16 B/hr ft F 73.75 cal/hr cm C 1.53x10 ⁸ CAL ³ /hr N	(5)
Diffusivity (a)			.49 ft ² /hr 455 cm ² /hr 530 CAL ² /hr	(5)
Equivalent Film Thickness (k/ \bar{h})		8.67x10 ⁻³ ft .264 cm 1.0 CAL		Construction
Maximum Slab Penetration			2.87x10 ⁻³ ft 8.71x10 ⁻² cm .33 CAL	nΔx (n = 10)
Distance Increment (Δx ₀) (Δx)		(Δx ₀) 8.67x10 ⁻³ ft .264 cm 1.0 CAL	(Δx) 2.87x10 ⁻⁴ ft 8.71x10 ⁻³ cm .033 CAL	Δx ₀ = x/ \sqrt{h} Δx = (2 a Δt _e) ^{1/2}
Time Increment (Δt) _e		.003 sec	.003 sec	(13)

The program entry employed with the HP-97 is given below. Any consistent system of units is suitable.

Primary Registers	Initial Values	Example
R_a	T_o^n	5596 F
R_B	T_n^o	70 F
R_1	t_e	8.33×10^{-7} hr
R_2	10	10
R_3	\bar{h}	1845 B/hr ft ² F
R_4	k	16 B/hr ft F
R_5	a	.49 ft ² /hr

Output after 3-millisecond time exposure

$T_{11} = T_{12}$	246 F
$T_{13} = T_{14}$	331 F
$T_{15} = T_{16}$	394 F
$T_{17} = T_{18}$	446 F
$T_{19} = T_{110}$	490 F

PROGRAM LISTING

001	*LBLA	21 11	041	+	-55	091	x	-35
002	PREG	16-13	042	PRTX	-14	092	8	08
003	RCL1	36 01	043	RCL2	36 02	093	÷	-24
004	RCL2	36 02	044	X²	53	094	RCLB	36 12
005	÷	-24	045	STG5	35 09	095	+	-55
006	STOC	35 13	046	RCL2	36 02	096	PRTX	-14
007	RCL5	36 05	047	4	04	097	RCL9	36 09
008	x	-35	048	.	-62	098	X²	53
009	2	02	049	5	05	099	8	08
010	x	-35	050	x	-35	100	x	-35
011	JX	54	051	CHS	-22	101	STO7	35 07
012	STO1	35 01	052	RCL5	36 09	102	RCL9	36 09
013	RCL4	36 04	053	+	-55	103	CHS	-22
014	RCL3	36 03	054	7	07	104	6	06
015	÷	-24	055	.	-62	105	0	00
016	STOD	35 14	056	5	05	106	x	-35
017	RCL1	36 01	057	+	-55	107	RCL7	36 07
018	÷	-24	058	RCL4	36 04	108	+	-55
019	1	01	059	x	-35	109	STO7	35 07
020	+	-55	060	4	04	110	RCL9	36 09
021	1/X	52	061	÷	-24	111	1	01
022	STO2	35 02	062	RCLB	36 12	112	9	09
023	RCLA	36 11	063	+	-55	113	0	00
024	RCLB	36 12	064	PRTX	-14	114	x	-35
025	-	-45	065	RCL9	36 09	115	RCL7	36 07
026	STO3	35 03	066	RCL2	36 02	116	+	-55
027	RCL2	36 02	067	x	-35	117	STO7	35 07
028	x	-35	068	STO8	35 08	118	RCL2	36 02
029	STO4	35 04	069	CHS	-22	119	3	03
030	RCLB	36 12	070	STO7	35 07	120	2	02
031	+	-55	071	RCL9	36 09	121	5	05
032	PRTX	-14	072	6	06	122	x	-35
033	3	03	073	x	-35	123	CHS	-22
034	RCL2	36 02	074	+	-55	124	RCL7	36 07
035	-	-45	075	STO7	35 07	125	+	-55
036	RCL4	36 04	076	RCL2	36 02	126	STO7	35 07
037	x	-35	077	1	01	127	3	03
038	2	02	078	4	04	128	1	01
039	÷	-24	079	.	-62	129	5	05
040	RCLB	36 12	080	5	05	130	+	-55
			081	x	-35	131	RCL4	36 04
			082	CHS	-22	132	x	-35
			083	RCL7	36 07	133	1	01
			084	+	-55	134	2	02
			085	1	01	135	8	08
			086	7	07	136	÷	-24
			087	.	-62	137	RCLB	36 12
			088	5	05	138	+	-55
			089	+	-55	139	PRTX	-14
			090	RCL4	36 04	140	RTN	04

APPENDIX D

HEAT TRANSFER COEFFICIENT FROM EXPERIMENTAL DATA

APPENDIX D

HEAT TRANSFER COEFFICIENT FROM EXPERIMENTAL DATA

Given the conditions recorded in Table D-1, the HP-97 input/output and the complete program listing follows. This program contains a recursive feature such that the initial estimate of \bar{h} is used to calculate $T_{1,9}$, which is then compared with the experimental value, whereupon a recalculation using a modified value of \bar{h} is used to reform $T_{1,9}$ until it is within the acceptable range selected. The cyclic converging values of $T_{1,9}$ are printed in order, and the result presents the final \bar{h} with the corresponding temperature progression.

TABLE D-1. DEFINITION OF BOUNDARY CONDITIONS FOR EXPERIMENTAL PROPELLANT ROUND

	Heat Source	Film	Steel Slab	Reference
Initial Temperature (T_0)	4398 F 2425 C 2429 N	70 F 21 C 265 N	70 F 21 C 265 N	(12), (13)
Unit Film Conductance (\bar{h})		12000 B/hr ft ² F 1815 cal/hr cm ² C 4.23x10 ¹⁰ CAL ² /hr N		Assumed
Thermal Conductivity (k)			16 B/hr ft F 73.75 cal/hr cm C 4.23x10 ¹⁰ CAL/hr N	(5)
Diffusivity (a)			.49 ft ² /hr 455 cm ² /hr 2.77x10 ⁹ CAL ² /hr	(5)
Equivalent Film Thickness (k/ \bar{h})		1.33x10 ⁻³ ft .0406 cm 1.0 CAL		Construction
Maximum Slab Penetration			1.38x10 ⁻³ ft .042 cm 1.04 CAL	nΔx (n = 10)
Distance Increment (Δx ₀)		(Δx ₀) 1.33x10 ⁻³ ft .0406 cm	(Δx) 1.38x10 ⁻⁴ ft .0042 cm	Δx ₀ = k/ \bar{h} Δx = (2 a $\frac{\Delta t_e}{n}$) ^{1/2}
Time Increment (Δt) _e		.0007 sec	.0007 sec	(13)

HP-97 INITIAL REGISTER CONTENTS

Register 0 enters the range of temperature convergence.

Register 1 is the elapsed time in hours.

Register 2 is 10

Register 3 allows the estimate of \bar{h} , the film coefficient.

Register 4 gives k , the conductivity of the metal wall.

Register 5 indicates a , the diffusivity of the metal wall.

Registers 6 - 9 are zero

Register A is the driving gas temperature T_{0n} , usually taken as the local adiabatic flame temperature.

Register B is the initial wall temperature T_{10} .

Registers 6, D and E are zero.

Register I gives the wall temperature rise in °C. If the calculation is not carried out in British units, steps 153 to 159 in the listing must be adjusted to delete the conversion of T_{10} from °F to °C.

OUTPUT

The intermediate printout is the temperature rise for each permutation of h . For a slowly converging operation, the program can be stopped at any point and a revised h entered in Register 3.

The final printout gives the complete results of the terminal calculation.

Register 0 shows \bar{h} .

Register 1 gives T_{11} .

Register 2 gives T_{13} .

Register 3 gives T_{15} .

Register 4 gives T_{17} .

Register 5 gives T_{19} .

Register 6 repeats Register I.

Registers 7 - 9 are zero.

Register A repeats the driving gas temperature T_o .

Register B repeats the initial wall temperature T_{1o} .

Registers C and D have no significance to the result.

Registers E and I present the final calculated and the reference temperature rise respectively.

The actual program entry is given below. With the exception noted for Register I, any consistent system of units is suitable.

Primary Registers	Initial Values	Example
R ₀	T _z	2 C
R ₁	t _e	1.94x10 ⁻⁷ hr
R ₂	Constant	10
R ₃	\bar{h}	12000 B/hr ft ² F
R ₄	k	16 B/hr ft F
R ₅	a	.49 ft ² /hr
R ₆	0	0
R ₇	0	0
R ₈	0	0
R ₉	0	0
R _A	T _{0n}	4398 F
R _B	T ₁₀	70 F
R _C	0	0
R _D	0	0
R _E	0	0
R _I	T ₁₉ - T ₁₀	450 C

Intermediate values of

$$T_{19} - T_{10} (^{\circ}\text{C})$$

Output after iteration.

R ₀	\bar{h}	10953.2 B/hr ft ² F
R ₁	T ₁₁	410 F
R ₂	T ₁₃	567 F
R ₃	T ₁₅	678 F
R ₄	T ₁₇	767 F
R ₅	T ₁₉	842 F
R ₆	T ₁₉ - T ₁₁ (calc)	449.9 C
R ₇		0

R_8	--	0
R_9	--	0
R_A	T_{on}	4398 F
R_B	T_{10}	70 F
$R_{\bar{C}}$	--	--
R_D	--	--
R_E	$T_{10} - T_{10} \text{ (calc)}$	449.9 C
R_I	$T_{10} - T_{10} \text{ (ref)}$	450 C

PROGRAM LISTING

001	*LBLA	21 11
002	PREG	16-13
003	*LBLC	21 13
004	RCL1	36 01
005	RCL2	36 02
006	÷	-24
007	STOC	35 13
008	RCL5	36 05
009	x	-35
010	2	02
011	x	-35
012	IX	54
013	STOC	35 13
014	RCL4	36 04
015	RCL3	36 03
016	P2S	16-51
017	STOC	35 00
018	P2S	16-51
019	÷	-24
020	STOD	35 14
021	RCLC	36 13
022	÷	-24
023	1	01
024	+	-55
025	IX	52
026	STOD	35 14
027	RCLA	36 11
028	RCLB	36 12
029	-	-45
030	RCLD	36 14
031	x	-35
032	STOE	35 15
033	RCLB	36 12
034	+	-55
035	P2S	16-51
036	STO1	35 01
037	P2S	16-51
038	3	03
039	RCLD	36 14
040	-	-45
041	RCLC	36 13
042	x	-35
043	2	02
044	÷	-24
045	RCLB	36 12
046	+	-55
047	P2S	16-51
048	STO2	35 02
049	P2S	16-51
050	RCLD	36 14
051	X²	53
052	STO9	35 09
053	RCLD	36 14
054	4	04
055	.	-62
056	5	05
057	x	-35
058	CHS	-22
059	RCL9	36 09
060	+	-55
061	7	07
062	.	-62
063	5	05
064	+	-55
065	RCLC	36 13
066	x	-35
067	4	04
068	÷	-24
069	RCLB	36 12
070	+	-55
071	P2S	16-51
072	STO3	35 03
073	P2S	16-51
074	RCL9	36 09
075	RCLD	36 14
076	x	-35
077	STO6	35 06
078	CHS	-22
079	STO7	35 07
080	RCL9	36 09
081	6	06
082	x	-35
083	+	-55
084	STO7	35 07
085	RCLD	36 14
086	1	01
087	4	04
088	.	-62
089	5	05
090	^	-35
091	CHS	-22
092	RCL7	36 07
093	+	-55
094	1	01
095	7	07

096	.	-62							
097	5	05							
098	+	-55							
099	RCLC	36 15	139	1	01				
100	x	-35	140	5	05				
101	8	08	141	+	-55				
102	=	-24	142	RCLC	36 15	180	RCL3	36 03	
103	RCLB	36 12	143	x	-35	181	.	-62	
104	+	-55	144	1	01	182	9	09	
105	PzS	16-51	145	2	02	183	5	05	
106	ST04	35 04	146	8	08	184	=	-24	
107	PzS	16-51	147	=	-24	185	1	01	
108	RCL9	36 09	148	RCLB	36 12	186	0	00	
109	Xz	53	149	+	-55	187	0	00	
110	8	08	150	PzS	16-51	188	-	-45	
111	x	-35	151	ST05	35 05	189	ST03	35 03	
112	ST07	35 07	152	PzS	16-51	190	RCLC	36 15	
113	RCL8	36 08	153	3	03	191	RCLI	36 46	
114	CHS	-22	154	2	02	192	-	-45	
115	6	06	155	-	-45	193	Xz	53	
116	0	00	156	5	05	194	JX	54	
117	x	-35	157	x	-35	195	RCL0	36 00	
118	RCL7	36 07	158	9	09	196	XzY?	16-35	
119	+	-55	159	=	-24	197	GT0E	22 15	
120	ST07	35 07	160	ST0E	35 15	198	PzS	16-51	
121	RCL9	36 09	161	PRTX	-14	199	PREG	16-13	
122	1	01	162	PzS	16-51	200	PzS	16-51	
123	9	09	163	ST06	35 06	201	RTN	24	
124	0	00	164	PzS	16-51	202	*LBLC	21 15	
125	x	-35	165	RCLI	36 46	203	RCL3	36 03	
126	RCL7	36 07	166	-	-45	204	7	07	
127	+	-55	167	RCL0	36 00	205	0	00	
128	ST07	35 07	168	XzY?	16-35	206	-	-45	
129	RCLD	36 14	169	GT0B	22 12	207	ST03	35 03	
130	3	03	170	GT0D	22 14	208	PzS	16-51	
131	2	02	171	*LBLB	21 12	209	ST00	35 00	
132	5	05	172	RCL3	36 03	210	PzS	16-51	
133	x	-35	173	.	-62	211	RCLC	36 15	
134	CHS	-22	174	9	09	212	RCLI	36 46	
135	RCL7	36 07	175	5	05	213	-	-45	
136	+	-55	176	x	-35	214	Xz	53	
137	ST07	35 07	177	ST03	35 03	215	JX	54	
138	3	03	178	GT0C	22 13	216	RCL0	36 00	
			179	*LBLD	21 14	217	XzY?	16-35	
						218	GT0C	22 13	
						219	PzS	16-51	
						220	PREG	16-13	
						221	RTN	24	
						222	R/S	51	

APPENDIX E

ALGEBRAIC SPECIFICATION OF T_0^n

APPENDIX E

ALGEBRAIC SPECIFICATION OF T_0^n

The program labeled E-3 refers to the determination of the driving gas temperature according to the requirements of Table 3. Program E-4 similarly refers to Table 4. The example and data of Appendix D are used for illustration.

INITIAL REGISTER CONTENTS

For both programs:

R_1 enters the wall temperature at time 1.

R_2 gives the wall temperature at time 3.

R_3 indicates the wall temperature at time 5.

R_4 is the wall temperature at time 7.

R_5 enters the wall temperature at time 9.

OUTPUT

The corresponding driving gas temperatures are given in stated sequence.

Primary Registers	Initial Values	Example
R ₁	T ₁ 1	410 F
R ₂	T ₁ 3	567 F
R ₃	T ₁ 5	678 F
R ₄	T ₁ 7	767 F
R ₅	T ₁ 9	842 F

Output

Program E-3	T ₀ 1	820 F
	T ₀ 3	1751 F
	T ₀ 5	2056 F
	T ₀ 7	2275 F
	T ₀ 9	2430 F

Program E-4	T ₀ 1	820 F
	T ₀ 3	1751 F
	T ₀ 5	2468 F
	T ₀ 7	3278 F
	T ₀ 9	3469 F

PROGRAM LISTING E - 3

001	*LBLE	21 15	051	x	-35	101	RCL5	35 07
002	RCL1	35 01	052	RCL1	35 01	102	1	01
003	2	02	053	+	-55	103	6	02
004	x	-35	054	ST07	35 07	104	x	-35
005	PRTX	-14	055	RCL3	35 03	105	RCL7	35 07
006	RCL2	35 02	056	8	08	106	+	-55
007	2	02	057	x	-35	107	ST07	35 07
008	x	-35	058	RCL7	35 07	108	RCL4	35 04
009	ST07	35 07	059	+	-55	109	6	06
010	RCL1	35 01	060	RCL1	35 01	110	4	04
011	3	03	061	x	-35	111	x	-35
012	x	-35	062	ST00	35 00	112	RCL7	35 07
013	RCL7	35 07	063	RCL1	35 01	113	+	-55
014	-	-45	064	1	01	114	RCL1	35 01
015	ST00	35 00	065	7	07	115	x	-35
016	RCL1	35 01	066	x	-35	116	ST00	35 00
017	X ²	55	067	ST07	35 07	117	RCL1	35 01
018	RCL0	35 00	068	RCL2	35 02	118	1	01
019	÷	-24	069	2	02	119	3	03
020	PRTX	-14	070	x	-35	120	3	03
021	RCL2	35 02	071	RCL7	35 07	121	x	-35
022	4	04	072	+	-55	122	ST07	35 07
023	x	-35	073	ST07	35 07	123	RCL2	35 02
024	RCL1	35 01	074	RCL3	35 03	124	8	08
025	+	-55	075	8	08	125	x	-35
026	RCL1	35 01	076	x	-35	126	RCL7	35 07
027	x	-35	077	RCL7	35 07	127	+	-55
028	ST00	35 00	078	+	-55	128	ST07	35 07
029	RCL1	35 01	079	ST07	35 07	129	RCL3	35 03
030	9	09	080	RCL4	35 04	130	1	01
031	x	-35	081	1	01	131	6	06
032	ST07	35 07	082	6	06	132	x	-35
033	RCL2	35 02	083	x	-35	133	RCL7	35 07
034	4	04	084	CH5	-22	134	+	-55
035	x	-35	085	RCL7	35 07	135	ST07	35 07
036	RCL7	35 07	086	+	-55	136	RCL4	35 04
037	+	-55	087	RCL0	35 00	137	6	06
038	ST07	35 07	088	÷	-24	138	4	04
039	RCL3	35 03	089	1/X	52	139	x	-35
040	8	08	090	PRTX	-14	140	RCL7	35 07
041	x	-35	091	RCL1	35 01	141	+	-55
042	CH5	-22	092	5	05	142	ST07	35 07
043	RCL7	35 07	093	x	-35	143	RCL5	35 05
044	+	-55	094	ST07	35 07	144	1	01
045	RCL0	35 00	095	RCL2	35 02	145	2	02
046	÷	-24	096	8	08	146	8	08
047	1/X	52	097	x	-35	147	x	-35
048	PRTX	-14	098	RCL7	35 07	148	CH5	-22
049	RCL2	35 02	099	+	-55	149	RCL7	35 07
050	2	02	100	ST07	35 07	150	+	-55
						151	RCL0	35 00
						152	÷	-24
						153	1/X	52
						154	PRTX	-14
						155	RTN	25

PROGRAM LISTING E-4

001	*LBLE	21 15	041	ST07	35 07	089	CHS	-22
002	RCL1	36 01	042	RCL2	36 02	090	RCL7	36 07
003	2	02	043	RCL3	36 03	091	+	-55
004	x	-35	044	x	-35	092	ST07	35 07
005	PRTX	-14	045	8	08	093	RCL2	36 02
006	RCL1	36 01	046	x	-35	094	RCL4	36 04
007	3	03	047	RCL7	36 07	095	x	-35
008	x	-35	048	+	-55	096	8	08
009	ST07	35 07	049	ST00	35 00	097	x	-35
010	RCL2	36 02	050	RCL1	36 01	098	RCL7	36 07
011	2	02	051	3	03	099	+	-55
012	x	-35	052	x	-35	100	ST07	35 07
013	RCL7	36 07	053	ST07	35 07	101	RCL3	36 03
014	-	-45	054	RCL2	36 02	102	x²	53
015	CHS	-22	055	1	01	103	8	08
016	ST00	35 00	056	0	00	104	x	-35
017	RCL1	36 01	057	x	-35	105	CHS	-22
018	x²	53	058	CHS	-22	106	RCL7	36 07
019	RCL0	36 00	059	RCL7	36 07	107	+	-55
020	÷	-24	060	+	-55	108	ST00	35 00
021	PRTX	-14	061	ST07	35 07	109	RCL4	36 04
022	RCL1	36 01	062	RCL3	36 03	110	1	01
023	4	04	063	8	08	111	6	06
024	x	-35	064	x	-35	112	x	-35
025	ST07	35 07	065	RCL7	36 07	113	ST07	35 07
026	RCL1	36 01	066	+	-55	114	RCL3	36 03
027	RCL2	36 02	067	RCL0	36 00	115	1	01
028	9	09	068	÷	-24	116	6	06
029	x	-35	069	1/X	52	117	x	-35
030	CHS	-22	070	PRTX	-14	118	CHS	-22
031	RCL7	36 07	071	RCL1	36 01	119	RCL7	36 07
032	+	-55	072	RCL3	36 03	120	+	-55
033	ST07	35 07	073	x	-35	121	RCL1	36 01
034	RCL2	36 02	074	CHS	-22	122	+	-55
035	x²	53	075	ST07	35 07	123	ST07	35 07
036	2	02	076	RCL1	36 01	124	RCL2	36 02
037	x	-35	077	RCL4	36 04	125	6	06
038	CHS	-22	078	x	-35	126	x	-35
039	RCL7	36 07	079	2	02	127	RCL7	36 07
040	+	-55	080	x	-35	128	+	-55
			081	RCL7	36 07	129	ST07	35 07
			082	+	-55	130	RCL3	36 03
			083	ST07	35 07	131	8	08
			084	RCL2	36 02	132	x	-35
			085	RCL3	36 03	133	CHS	-22
			086	x	-35	134	RCL7	36 07
			087	2	02	135	+	-55
			088	x	-35	136	RCL0	36 00
						137	÷	-24

138	1/X	52
139	PRTX	-14
140	RCL1	36 01
141	5	05
142	x	-35
143	ST07	35 07
144	RCL2	36 02
145	8	08
146	x	-35
147	RCL7	36 07
148	+	-55
149	ST07	35 07
150	RCL3	36 03
151	1	01
152	6	06
153	x	-35
154	RCL7	36 07
155	+	-55
156	ST07	35 07
157	RCL4	36 04
158	6	06
159	4	04
160	x	-35
161	RCL7	36 07
162	+	-55
163	RCL4	36 04
164	x	-35
165	CHS	-22
166	ST07	35 07
167	RCL1	36 01
168	8	08
169	x	-35
170	ST08	35 08
171	RCL2	36 02
172	1	01
173	6	06
174	x	-35
175	RCL8	36 08
176	+	-55
177	ST08	35 08
178	RCL3	36 03
179	6	06
180	4	04
181	x	-35
182	RCL8	36 08

183	+	-55
184	RCL5	36 05
185	x	-35
186	RCL7	36 07
187	+	-55
188	ST00	35 00
189	RCL5	36 05
190	6	06
191	4	04
192	x	-35
193	ST07	35 07
194	RCL2	36 02
195	4	04
196	x	-35
197	RCL7	36 07
198	+	-55
199	ST07	35 07
200	RCL3	36 03
201	2	02
202	4	04
203	x	-35
204	RCL7	36 07
205	+	-55
206	ST07	35 07
207	RCL4	36 04
208	9	09
209	6	06
210	x	-35
211	CHS	-22
212	RCL7	36 07
213	+	-55
214	2	02
215	x	-35
216	RCL1	36 01
217	5	05
218	x	-35
219	+	-55
220	RCL0	36 00
221	÷	-24
222	1/X	52
223	PRTX	-14
224	RTN	24

APPENDIX F
UNITS DESIGNATION

APPENDIX F

UNITS DESIGNATION

For the given examples, the properties are stated in the British, S.I. and normalized expression. The non-dimensional geometric "caliber" is most useful, with many applications in fluid dynamic analysis, and the extension to a normalized mass (weight) has been a convenience in rationalizing the performance of grossly different flight projectiles.^{F-1} Such manipulative procedures have physical limitations which are defined in the framework of their employment.

The normalization parameters are given below. Dividing weight (force) quantities by the specific weight of water converts them to length quantities and the mechanical equivalent of heat transforms heat units into mechanical units. In addition, this report introduces a common temperature (°Normalized) based on the absolute scale.

Length	$\frac{\text{linear dimension}}{\text{reference dimension}}$	CAL
Force	$\frac{\text{force}}{\text{specific weight of water} \times \text{ref dim}^3}$	CAL ³
Mass	$\frac{\text{mass}}{\text{specific mass of water} \times \text{ref dim}^3}$	CAL ³
Heat	$\frac{\text{heat} \times \text{mechanical equivalent}}{\text{specific weight of water} \times \text{ref dim}^4}$	CAL ⁴
Temperature	°Normalized = .9 °Kelvin = .5°Rankine	

^{F-1}W.F. Donovan, "One Factor Affecting the Dispersion of Long Rod Penetrators," ARBRL-MR-02846, June 1978. AD #A058596

LIST OF SYMBOLS

a	thermal diffusivity of metal wall
c	specific heat of metal wall
e	exponential constant
e	elapsed quantity (when appearing as a subscript)
\bar{h}	film heat transfer coefficient
j	natural logarithm of "r"
k	thermal conductivity of metal wall
m	$\frac{\Delta x}{\Delta x + \Delta x_0}$
n	sequential location of interstitial plane (appearing as subscript)
r	radius
τ	time
x	distance
cal	calorie
cm	centimeter
ft	foot
hr	hour
sec	second
B	British Thermal Unit
C	Centigrade
F	Fahrenheit
L	Length
N	Normalized
T	Temperature
CAL	Caliber
Δ	Difference indicator
Δt	Finite difference in time
ΔT	Finite difference in temperature
Δx	Finite difference in distance
ϕ	Operator defined as used in text
θ	Operator defined as used in text

LIST OF SYMBOLS (continued)

ρ	Density of medium
\dot{q}	Heat flux
r_i	Inner radius
r_o	Outer radius
t_e	Elapsed time
t_n	Time at n^{th} interstitial plane
t_z	Range of convergence for temperature calculation
T_n^t	Temperature at n^{th} interstitial plane at time "t"
Δx_o	Initial distance increment in Schmidt plot
ΔT_o	Initial driving temperature difference
HP-97	Hewlett Packard Model 97 Calculator
FORTTRAN	Computer language acronym for formula translation
CDC	CONTROL DATA CORPORATION
CALSPAN	Formerly Cornell Aeronautical Laboratory
SI	STANDARD INTERNATIONAL
BRL	BALLISTIC RESEARCH LABORATORY

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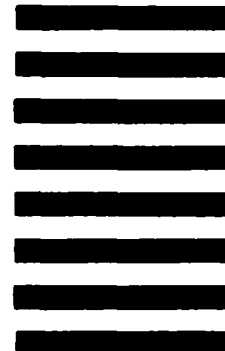


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